

The background of the slide is a dark blue gradient. It features a complex geometric pattern of thin, light blue lines. These lines form several sets of concentric circles, with some circles centered on the left and others on the right. Additionally, there are several straight lines that intersect these circles at various angles, creating a web-like or orbital pattern across the entire slide.

# **HHT Basics and Applications**

**For Speech, Machine Health Monitoring,  
and Bio-Medical Data Analysis**

**Norden E. Huang**

**March 24, 2003**

# Available Data Analysis Methods for **Nonstationary (but Linear)** time series

- **Various probability distributions**
- **Spectral analysis and Spectrogram**
- **Wavelet Analysis**
- **Wigner-Ville Distributions**
- **Empirical Orthogonal Functions aka Singular Spectral Analysis**
- **Moving means**
- **Successive differentiations**

# Available Data Analysis Methods for **Nonlinear** **(but Stationary and Deterministic)** time series

- **Phase space method**
  - **Delay reconstruction and embedding**
  - **Poincaré surface of section**
  - **Self-similarity, attractor geometry & fractals**
- **Nonlinear Prediction**
- **Lyapunov Exponents for stability**

HHT, for **Nonstationary, Nonlinear and Stochastic data**, consists of the following components:

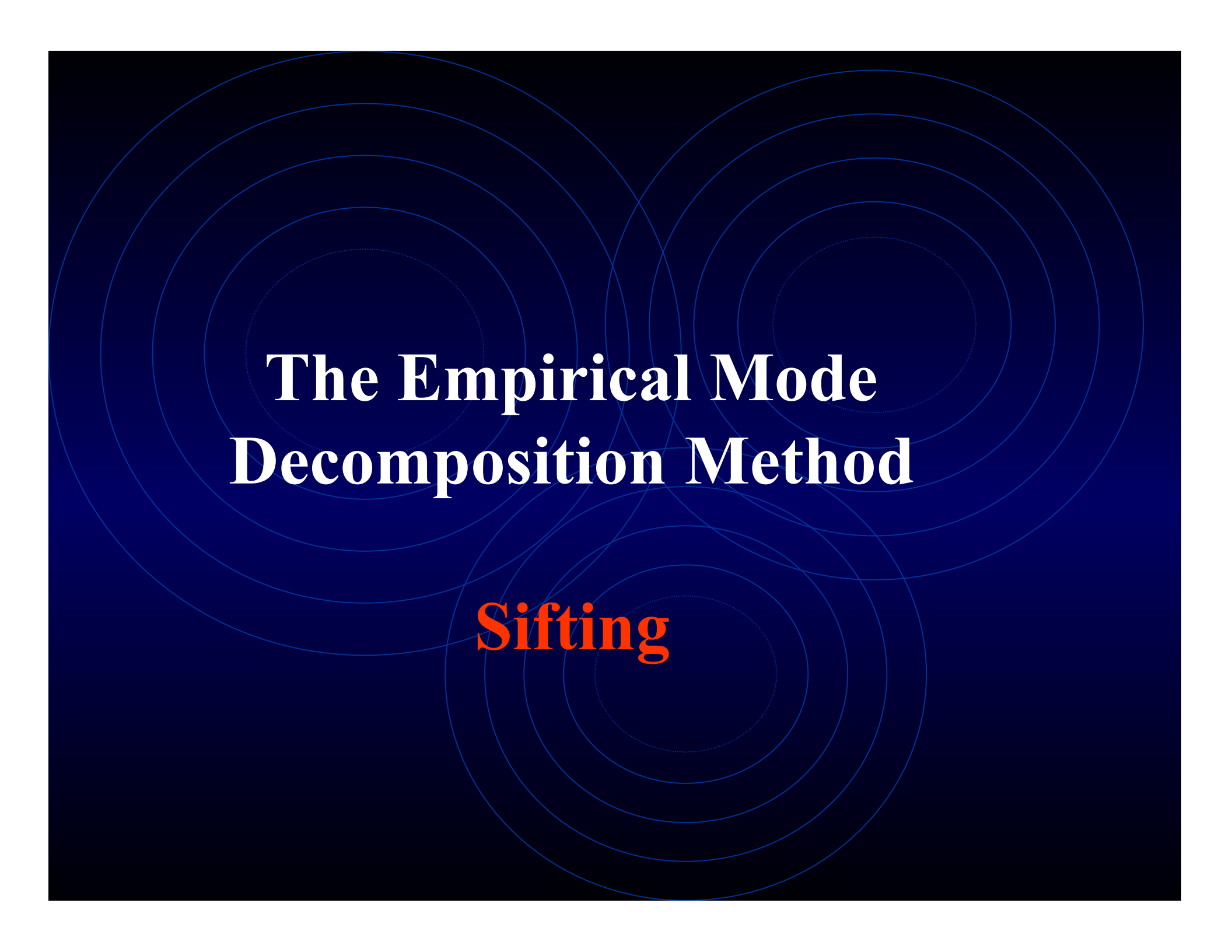
### **The Empirical Mode Decomposition:**

To generate the adaptive basis, the Intrinsic Mode Functions (IMF), from the data

### **The Hilbert Spectral Analysis:**

To generate a time-frequency-energy representation of the data Based on the IMFs



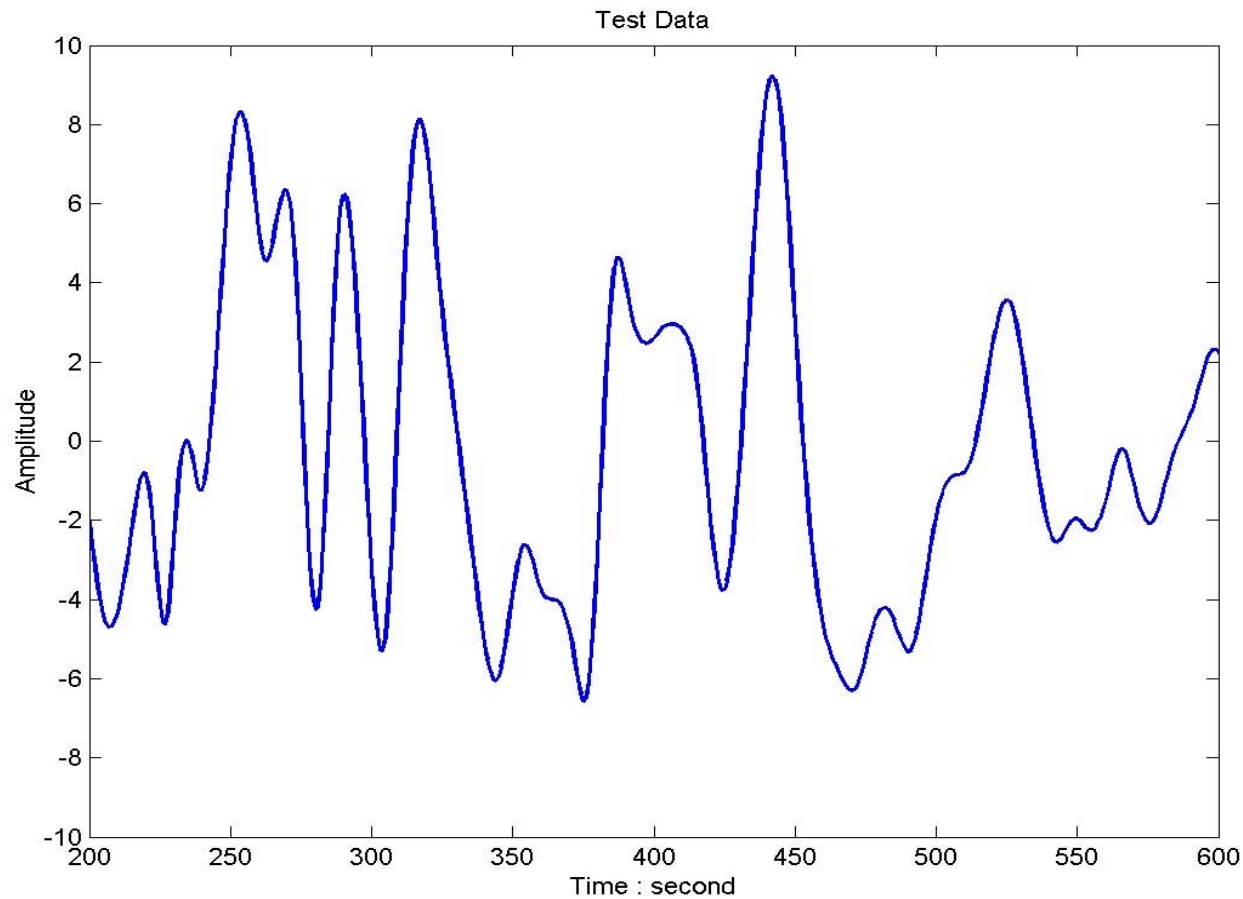
The background of the slide is a dark blue gradient. It features three sets of concentric circles in a lighter blue color. One set is on the left, one is on the right, and one is at the bottom center. The circles are thin and overlap each other.

# **The Empirical Mode Decomposition Method**

## **Sifting**

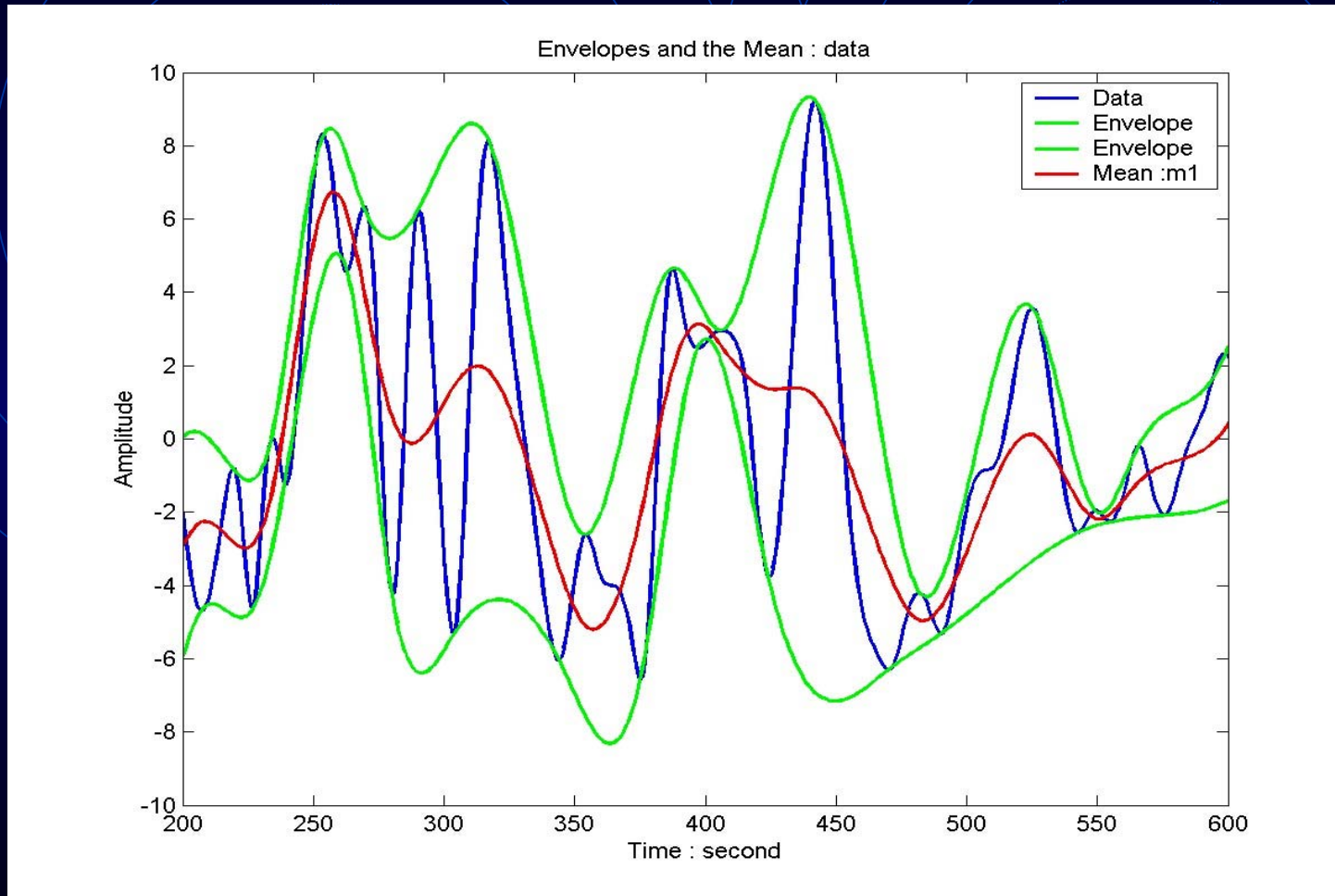
# Empirical Mode Decomposition:

## Methodology : Test Data



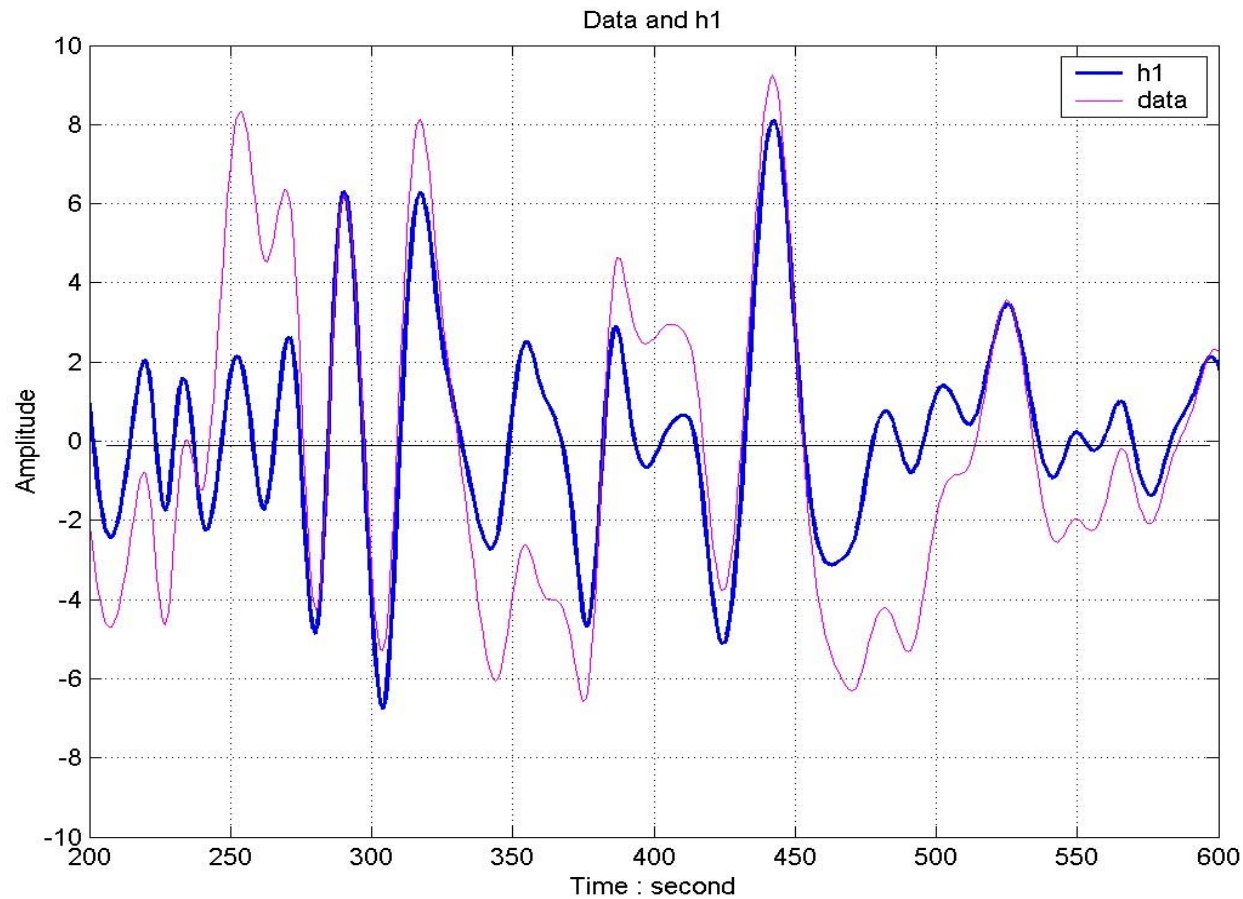
# Empirical Mode Decomposition:

## Methodology : data and m1



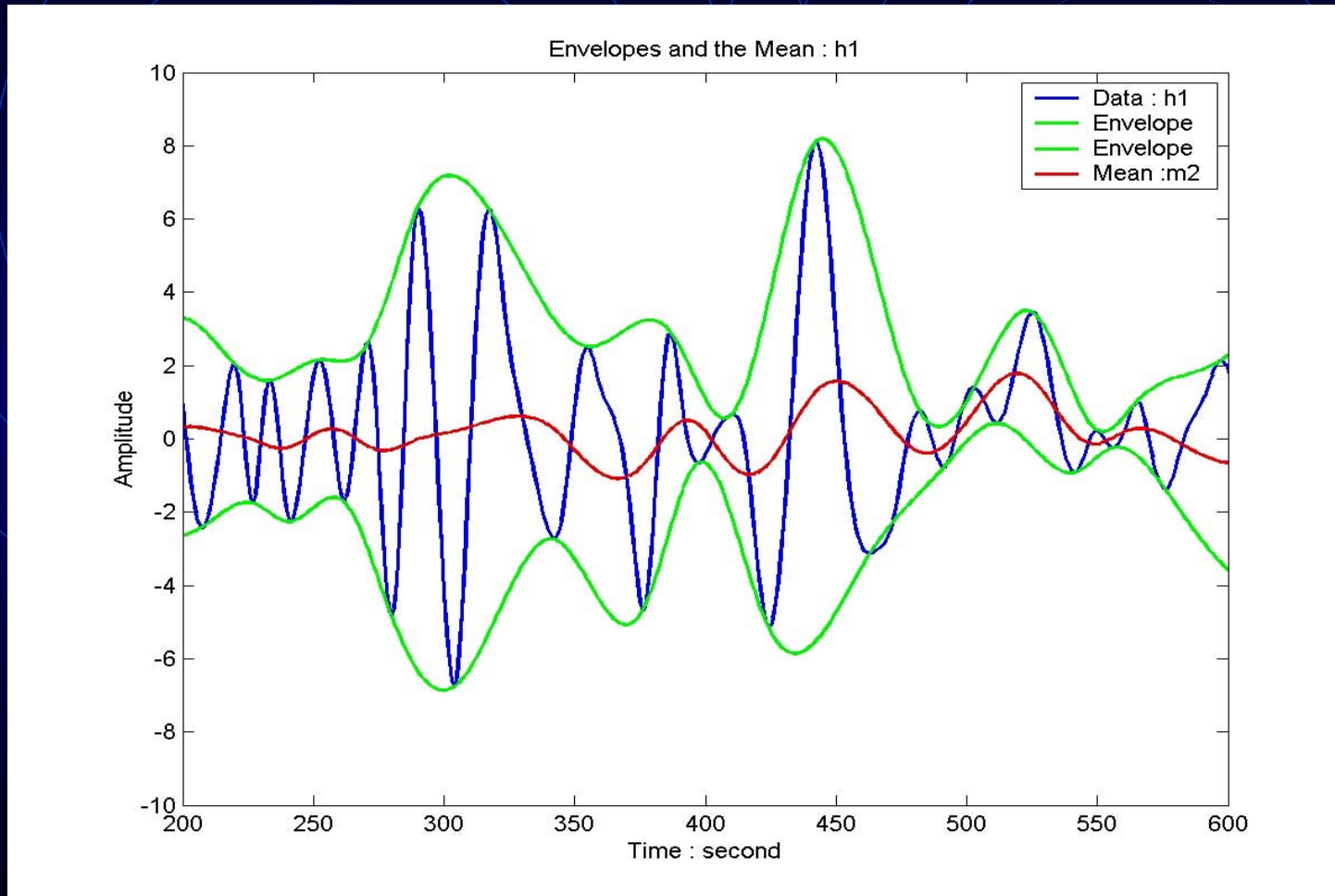
# Empirical Mode Decomposition:

## Methodology : data & h1



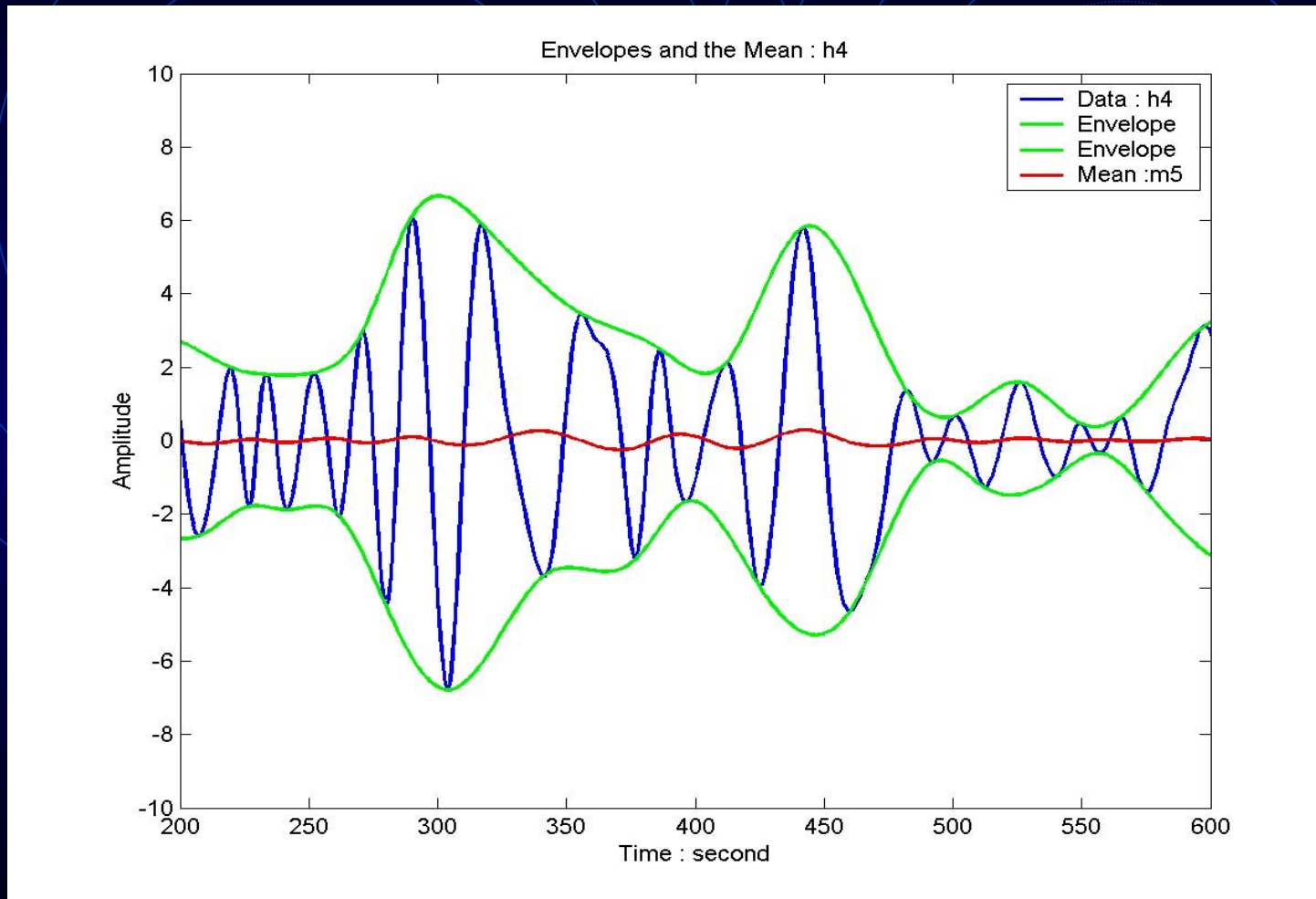
# Empirical Mode Decomposition:

## Methodology : h1 & m2



# Empirical Mode Decomposition:

## Methodology : h4 & m5



# Empirical Mode Decomposition

*Sifting : to get one IMF component*





## Two Stoppage Criteria : S and SD

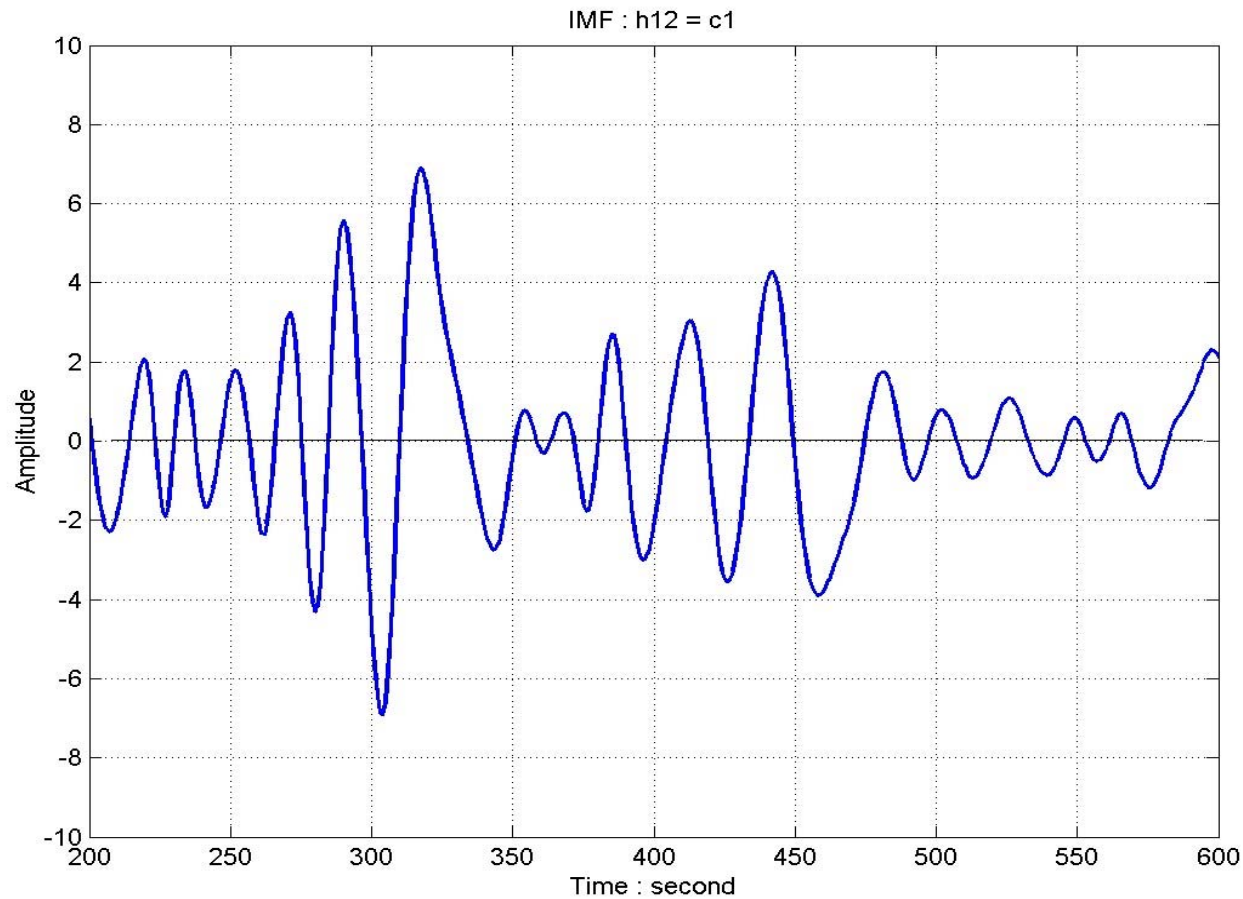
- The S number : S is defined as the consecutive number of siftings, in which the numbers of zero-crossing and extrema are the same for these S siftings.
- B. SD is small than a pre-set value, where





# Empirical Mode Decomposition:

## Methodology : IMF c1



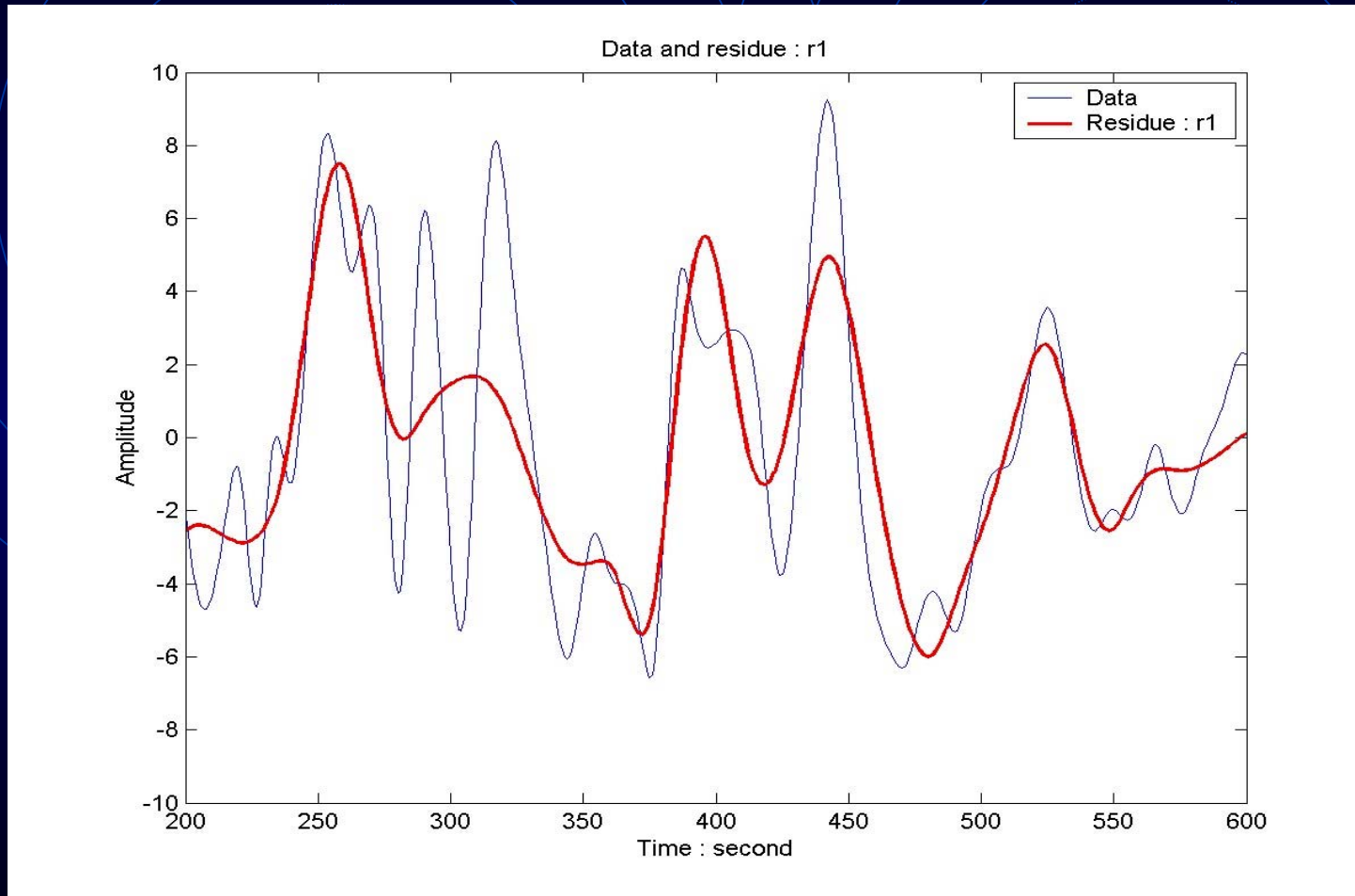
# Empirical Mode Decomposition

*Sifting : to get all the IMF components*



# Empirical Mode Decomposition:

## Methodology : data & r1



# Hilbert Transform : Definition

$$f(x) = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{f(t)}{x-t} dt$$

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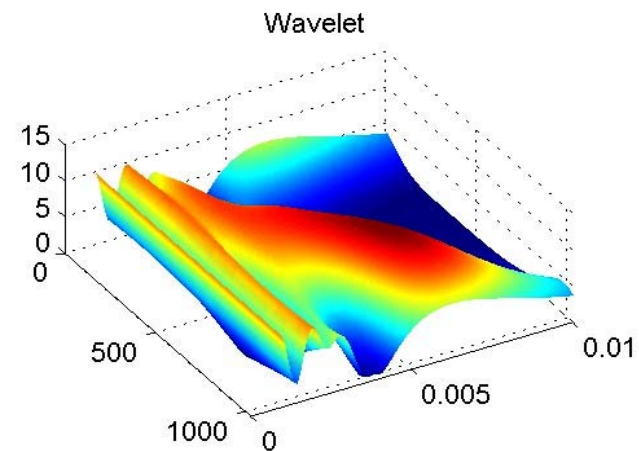
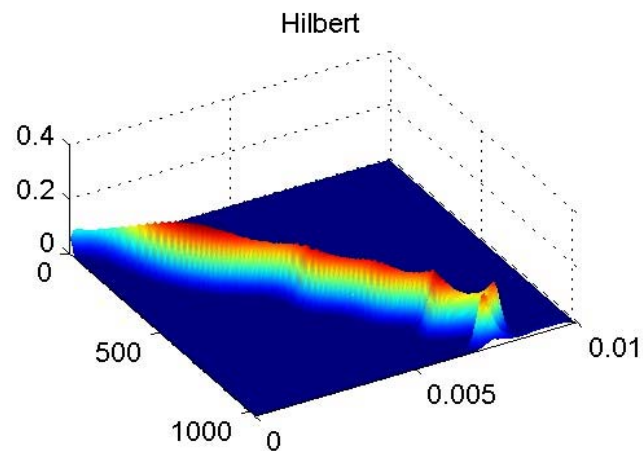
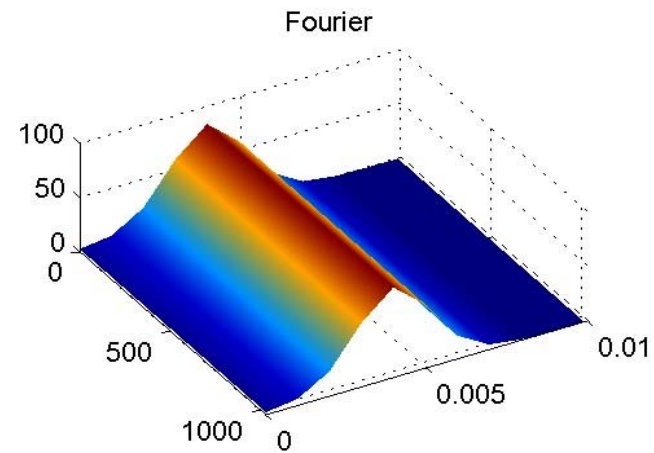
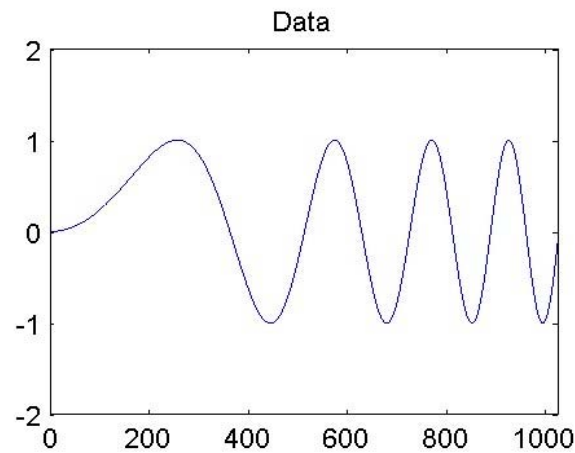
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# Comparison between FFT and HHT

12/11/2017

# Comparisons: Fourier, Hilbert & Wavelet

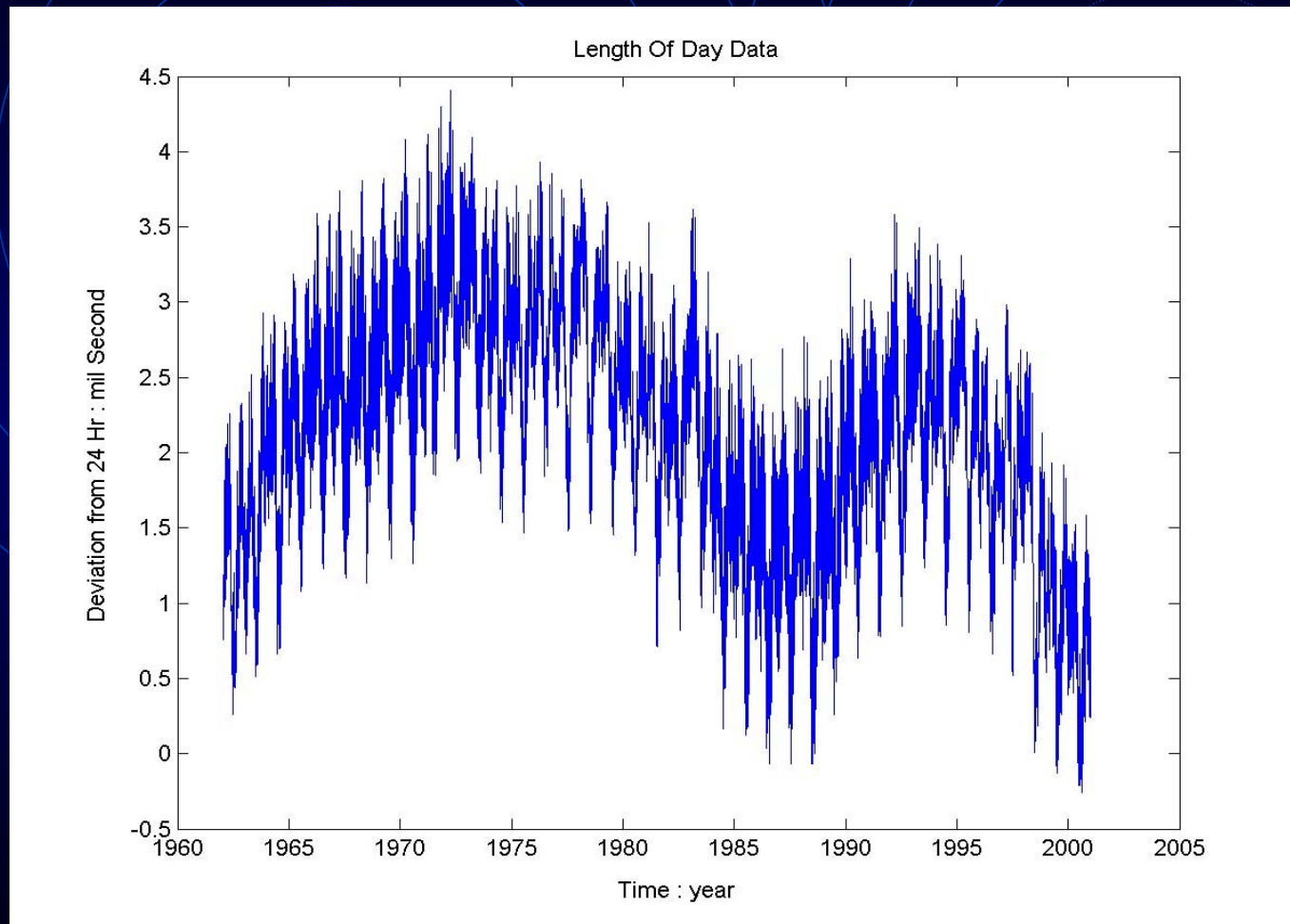
Comparison among Fourier, Hilbert, and Morlet Wavelet Spectra



The background is a dark blue gradient. Overlaid on this are three sets of concentric circles, each consisting of four thin, light blue lines. The circles are arranged in a triangular pattern, with one set in the top left, one in the top right, and one centered at the bottom. They overlap with each other and with the central text.

# **An Example of Sifting**

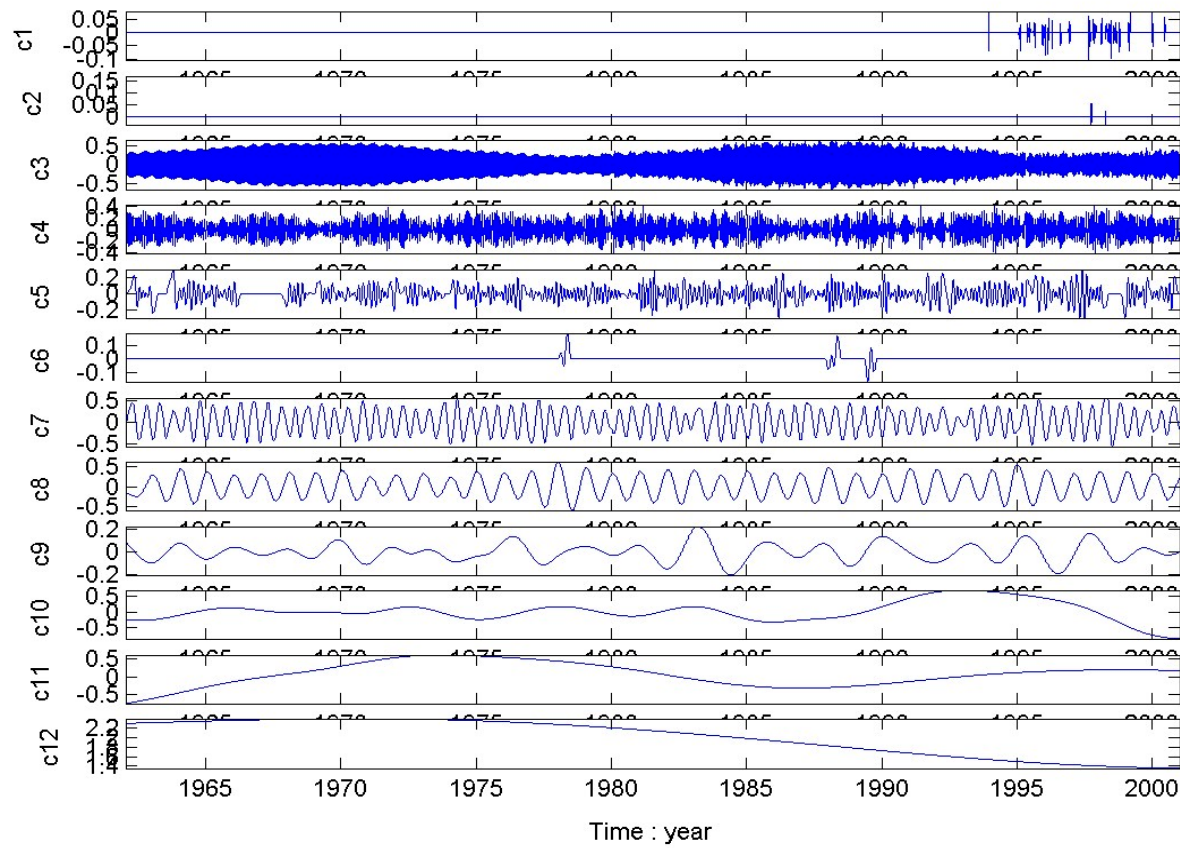
# Length Of Day Data



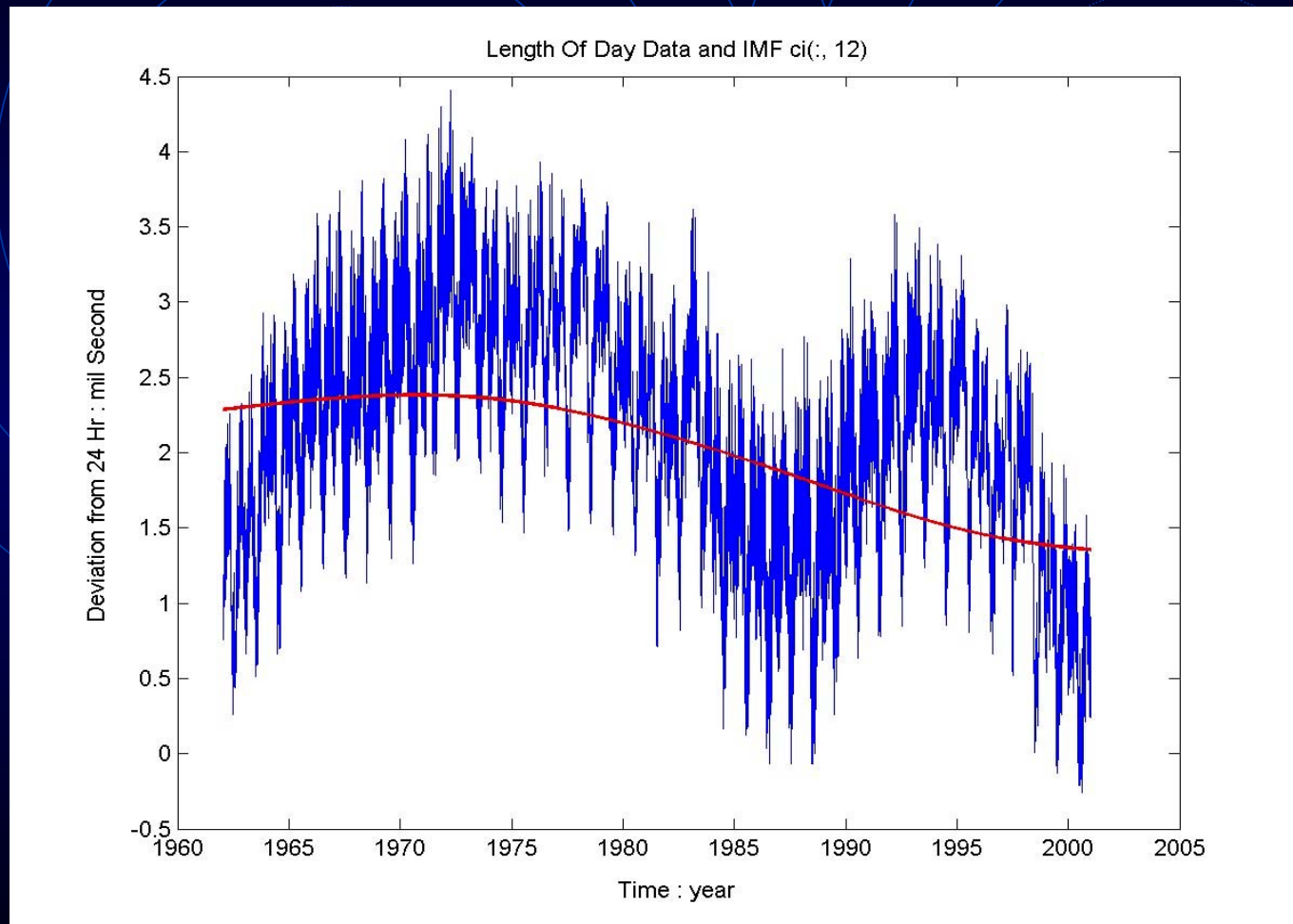


# LOD : IMF

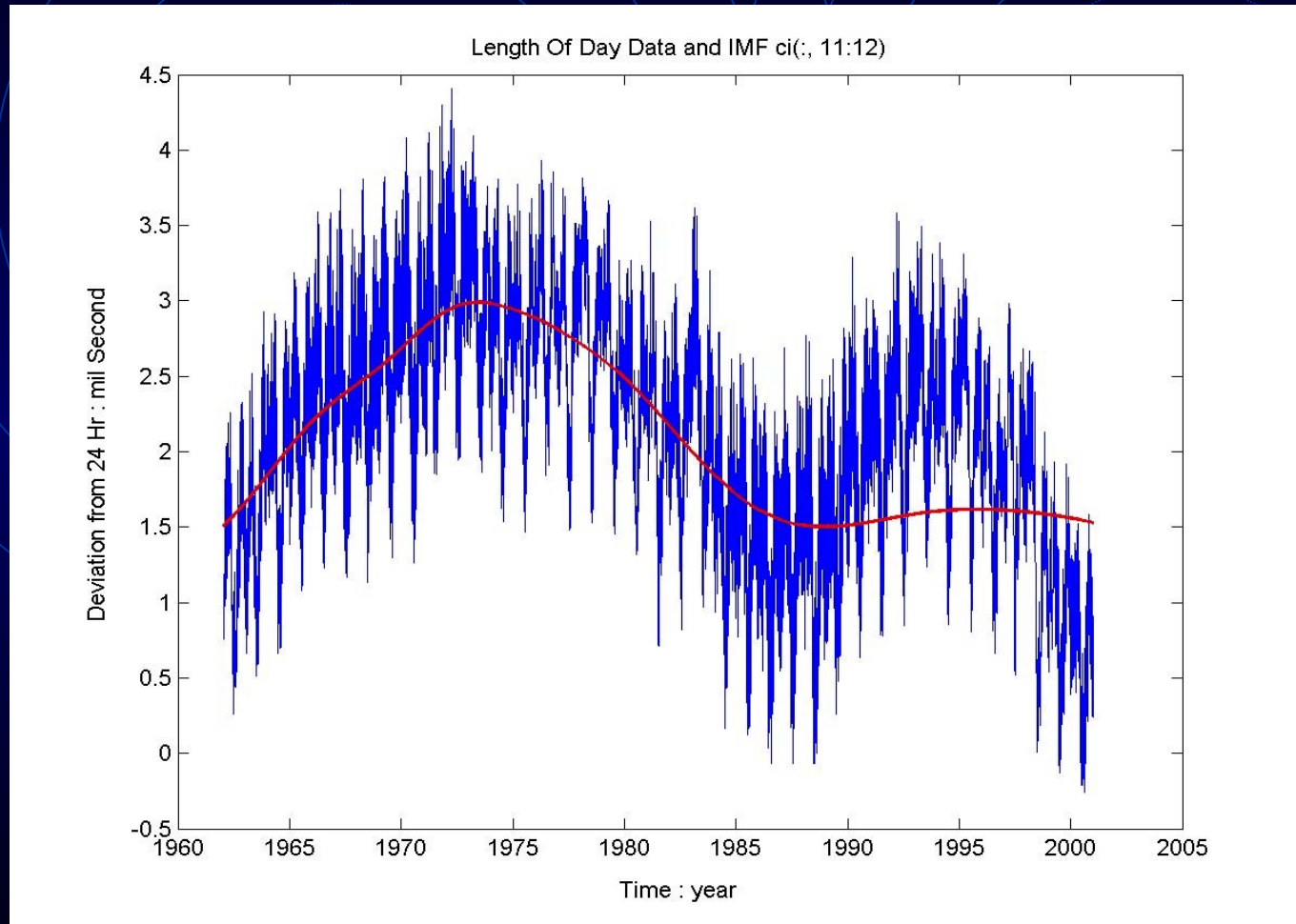
IMF LOD62 : ci(100,8,8; 3<sup>a</sup>,: 50,3,3;-1<sup>2</sup>,45<sup>a</sup>, -10)



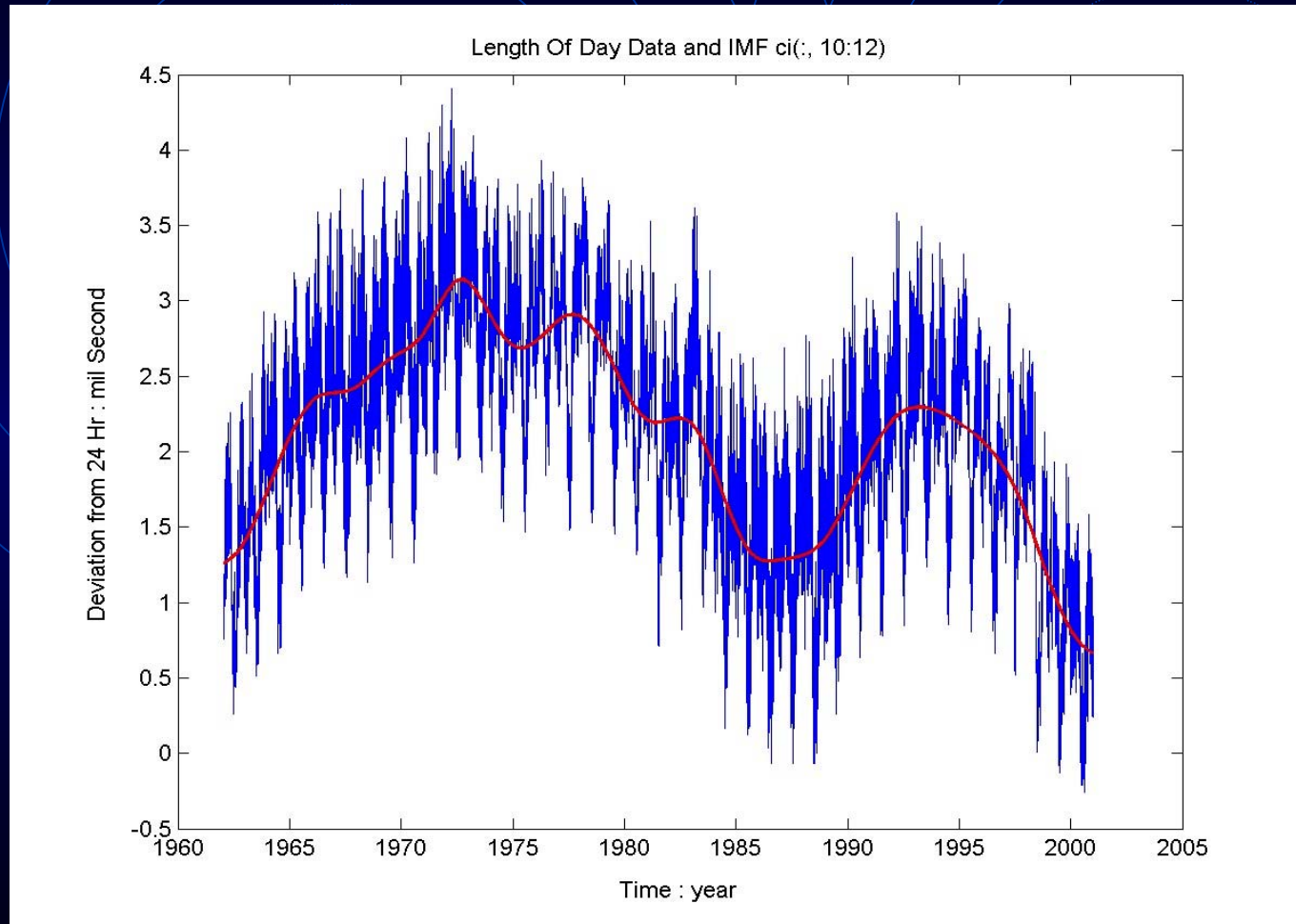
# LOD : Data & c12



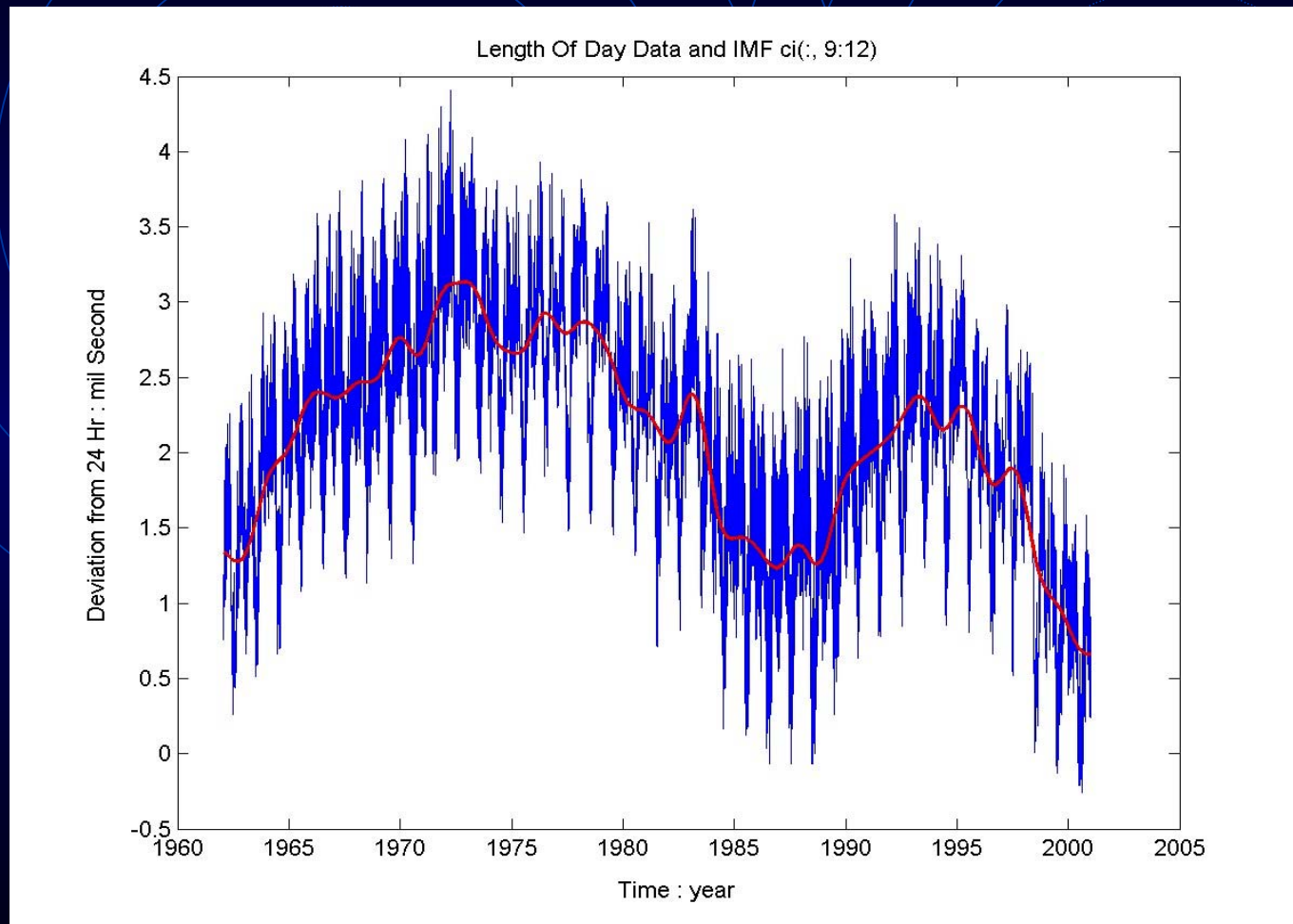
# LOD : Data & Sum c11-12



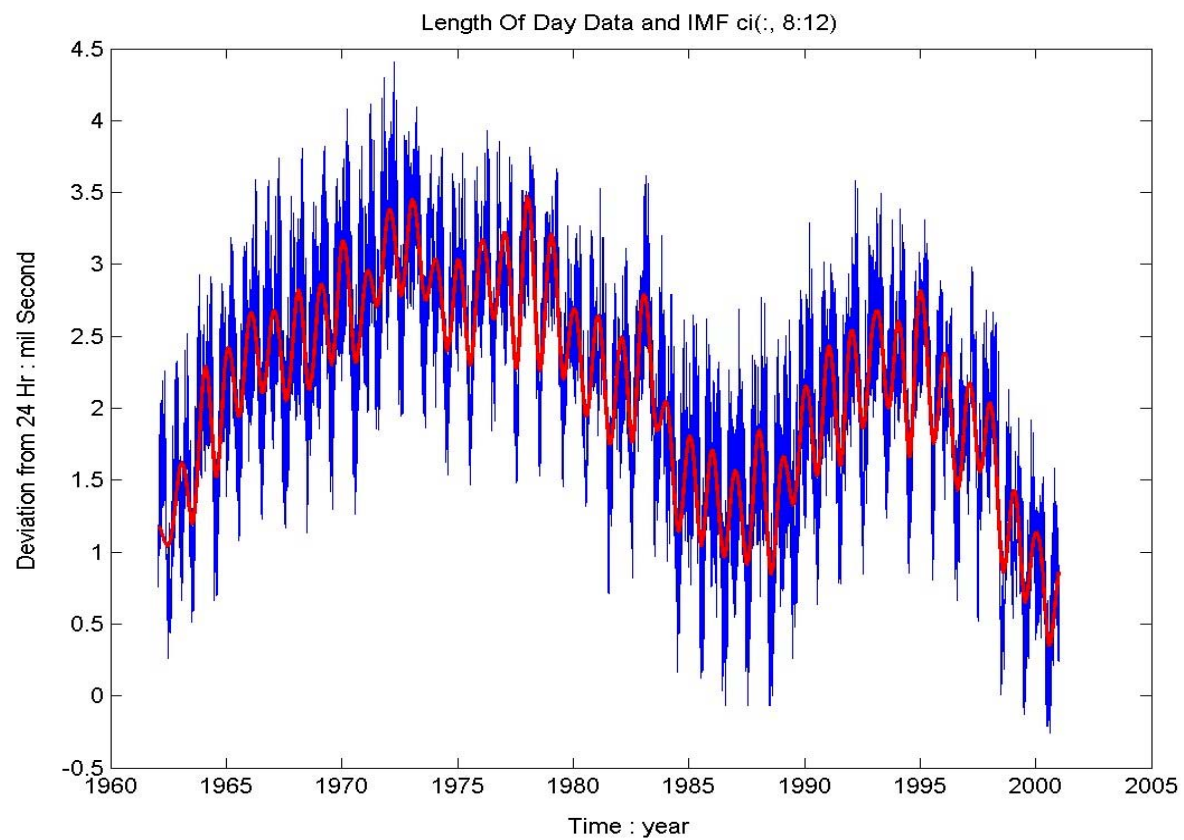
# LOD : Data & sum c10-12



# LOD : Data & c9 - 12

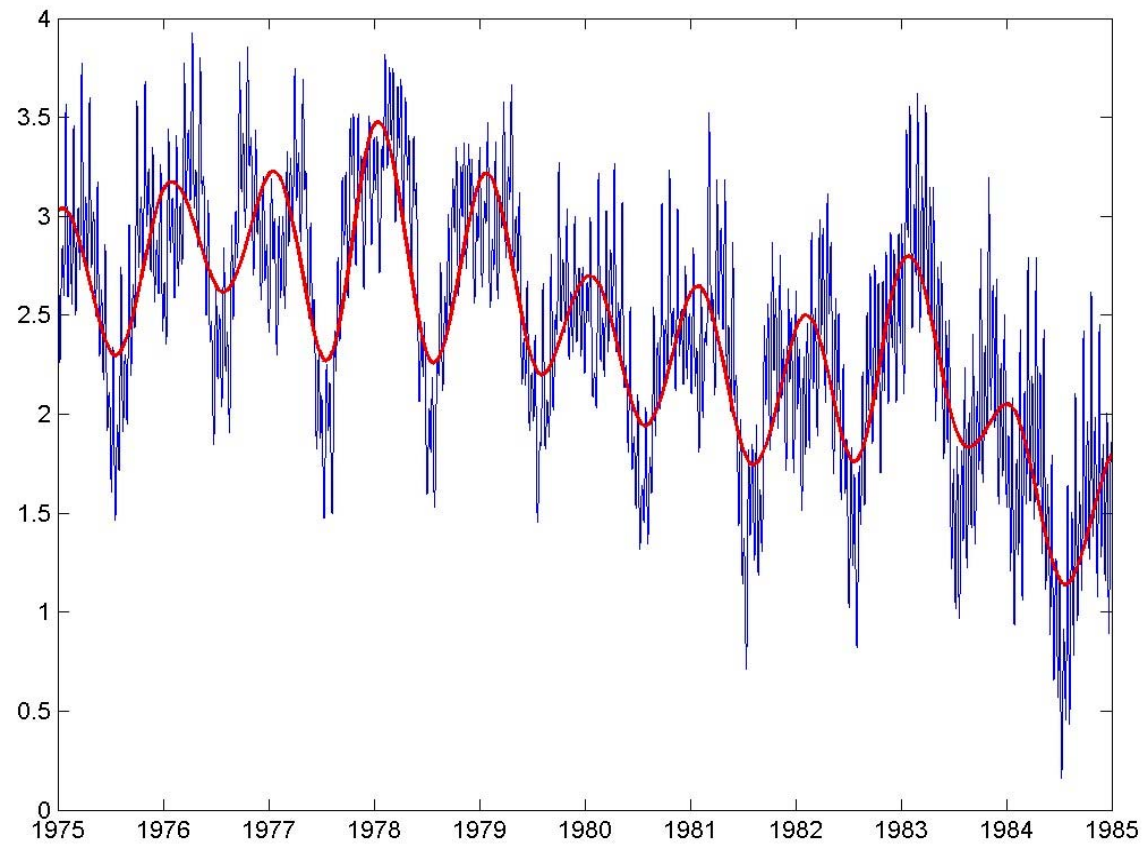


# LOD : Data & c8 - 12

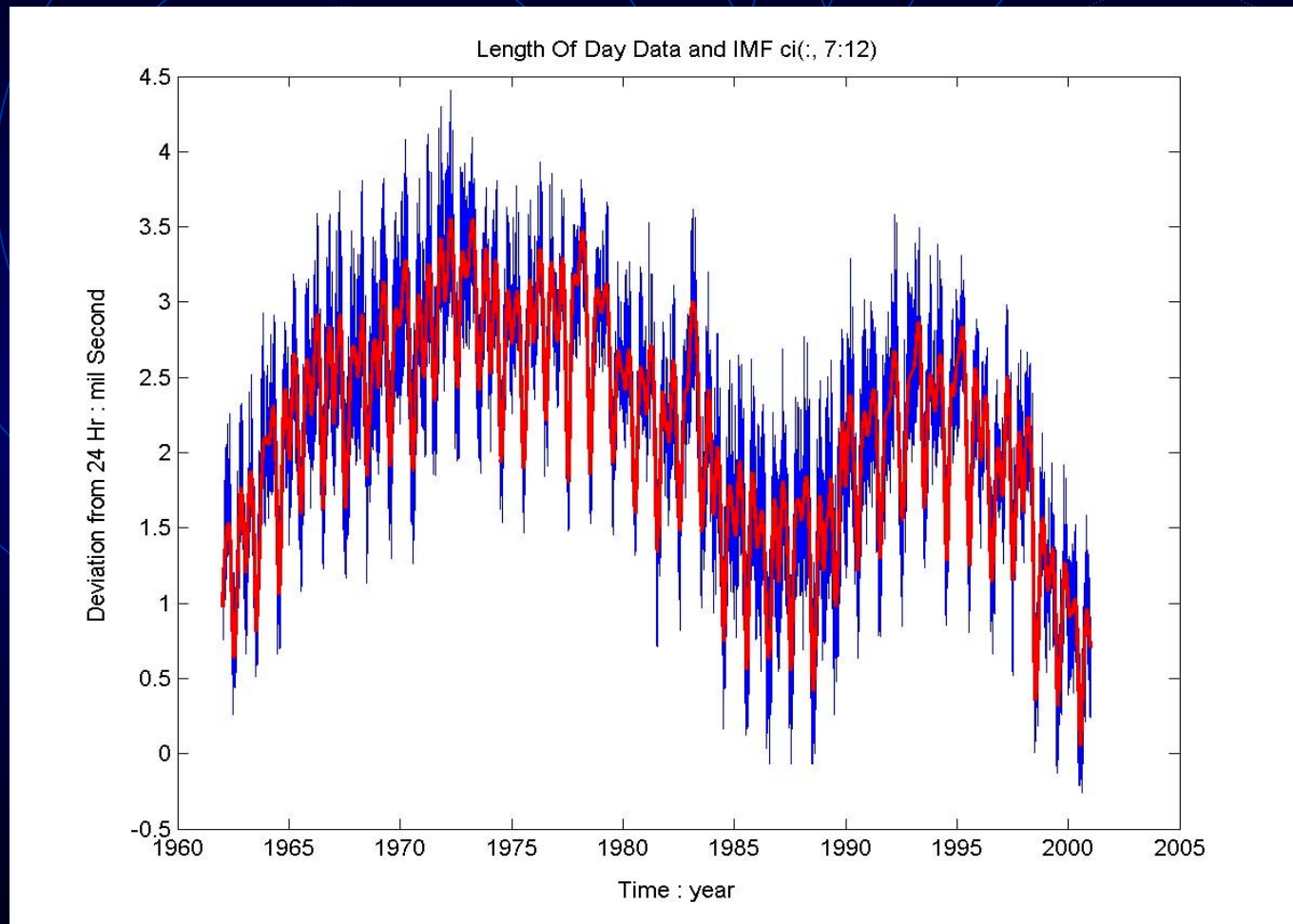




# LOD : Detailed Data and Sum c8-c12

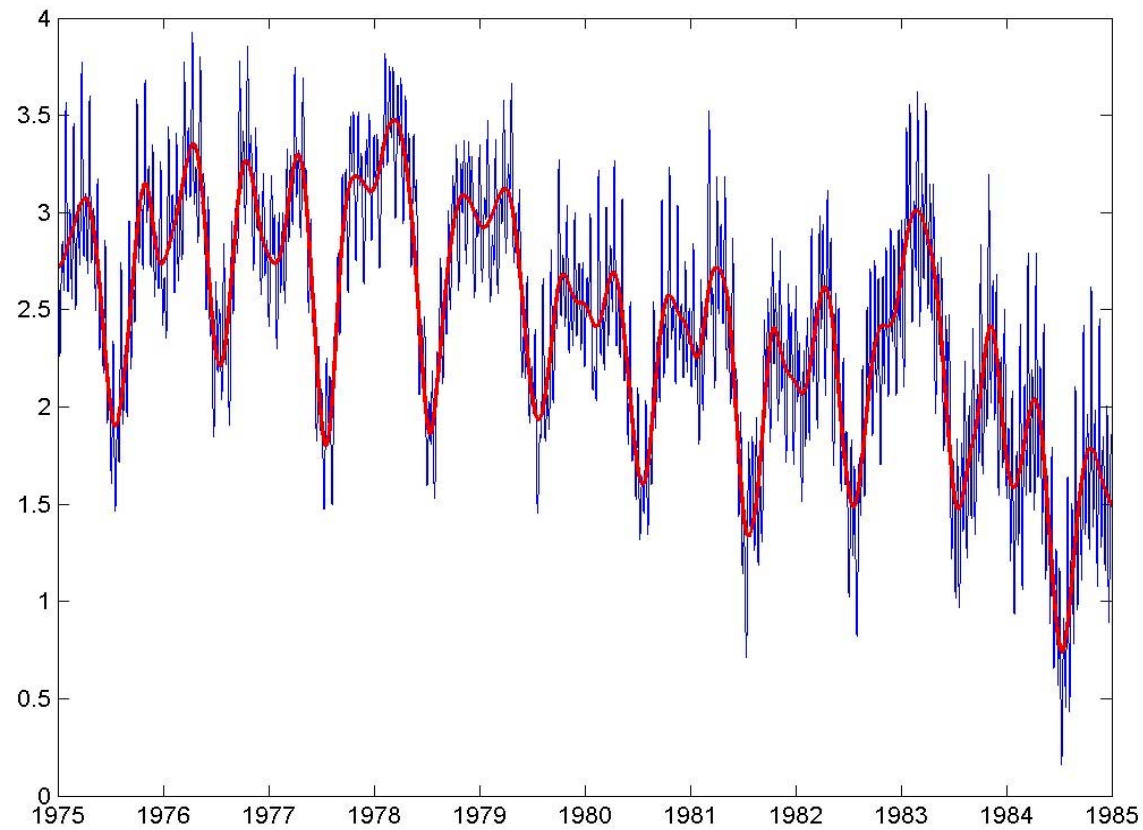


# LOD : Data & c7 - 12

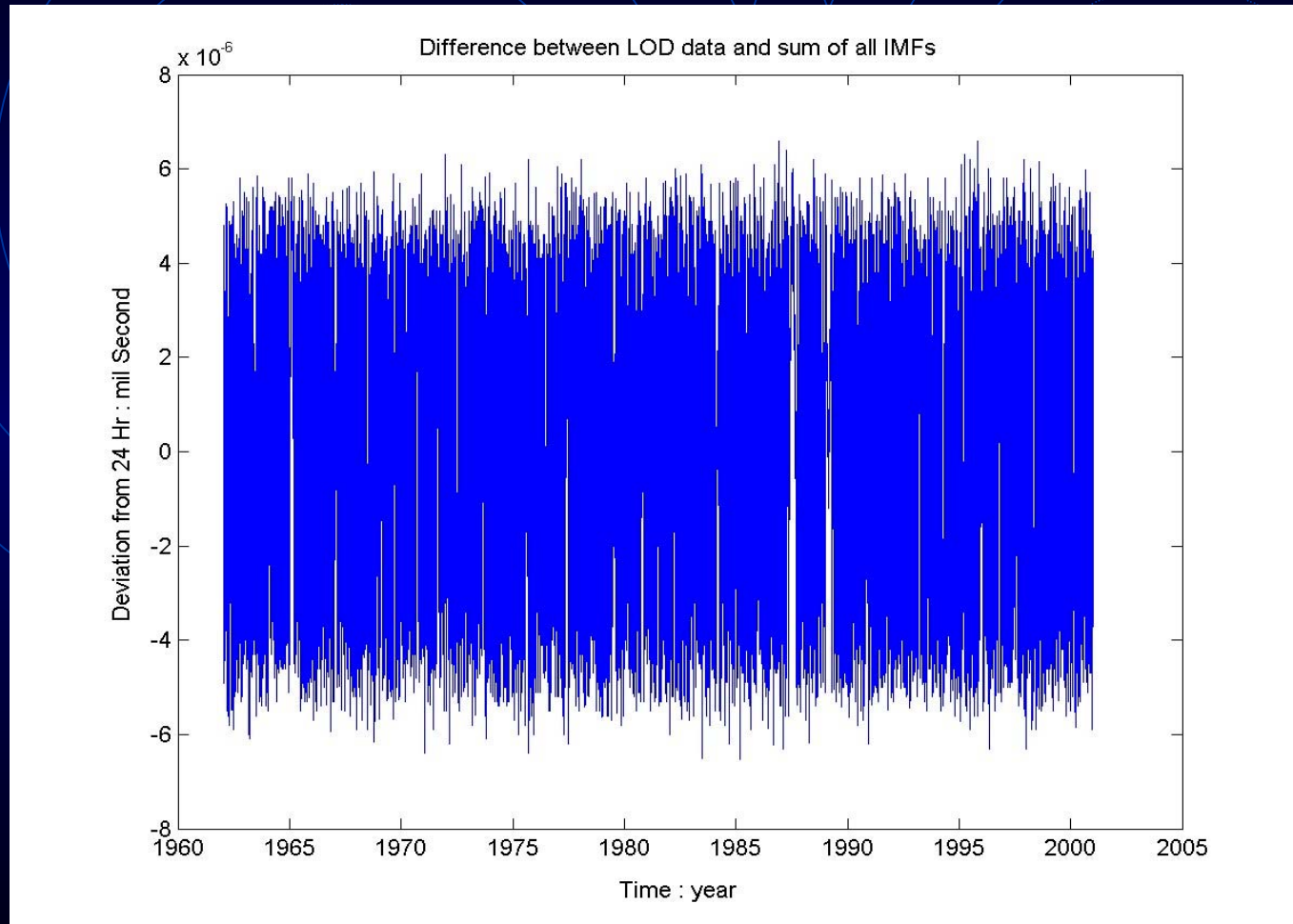




# LOD : Detail Data and Sum IMF c7-c12

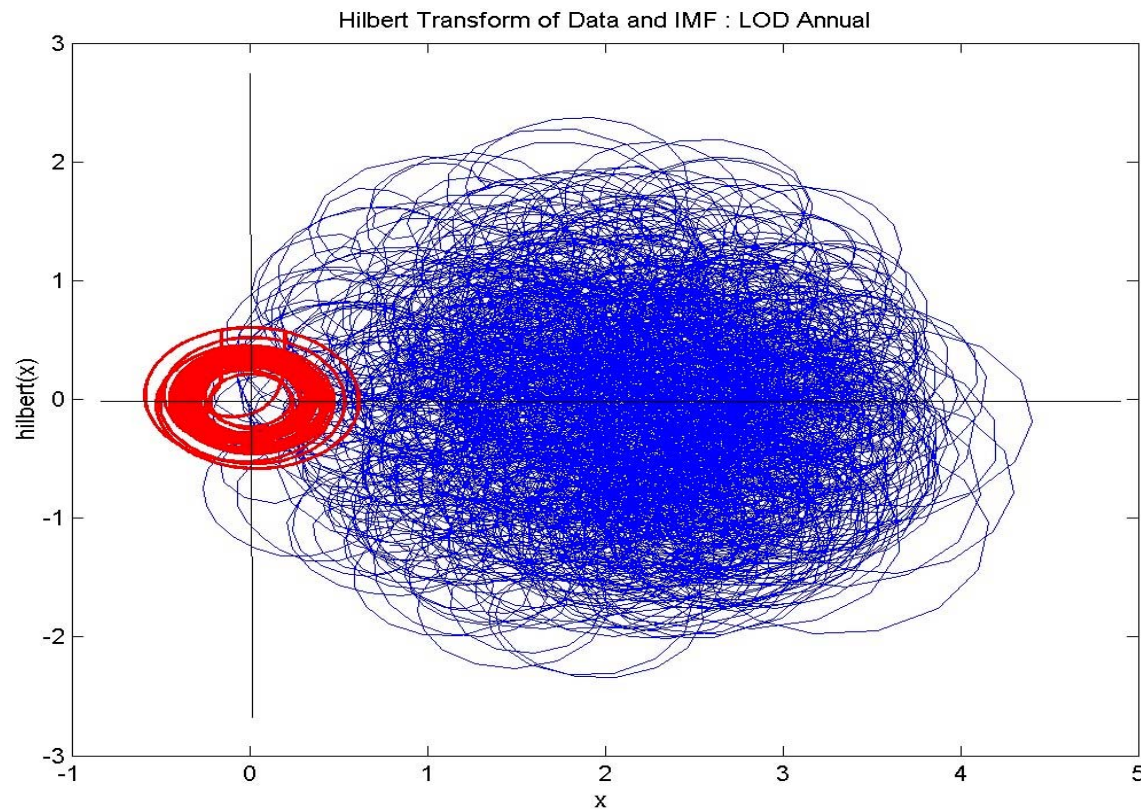


# LOD : Difference Data – sum all IMFs

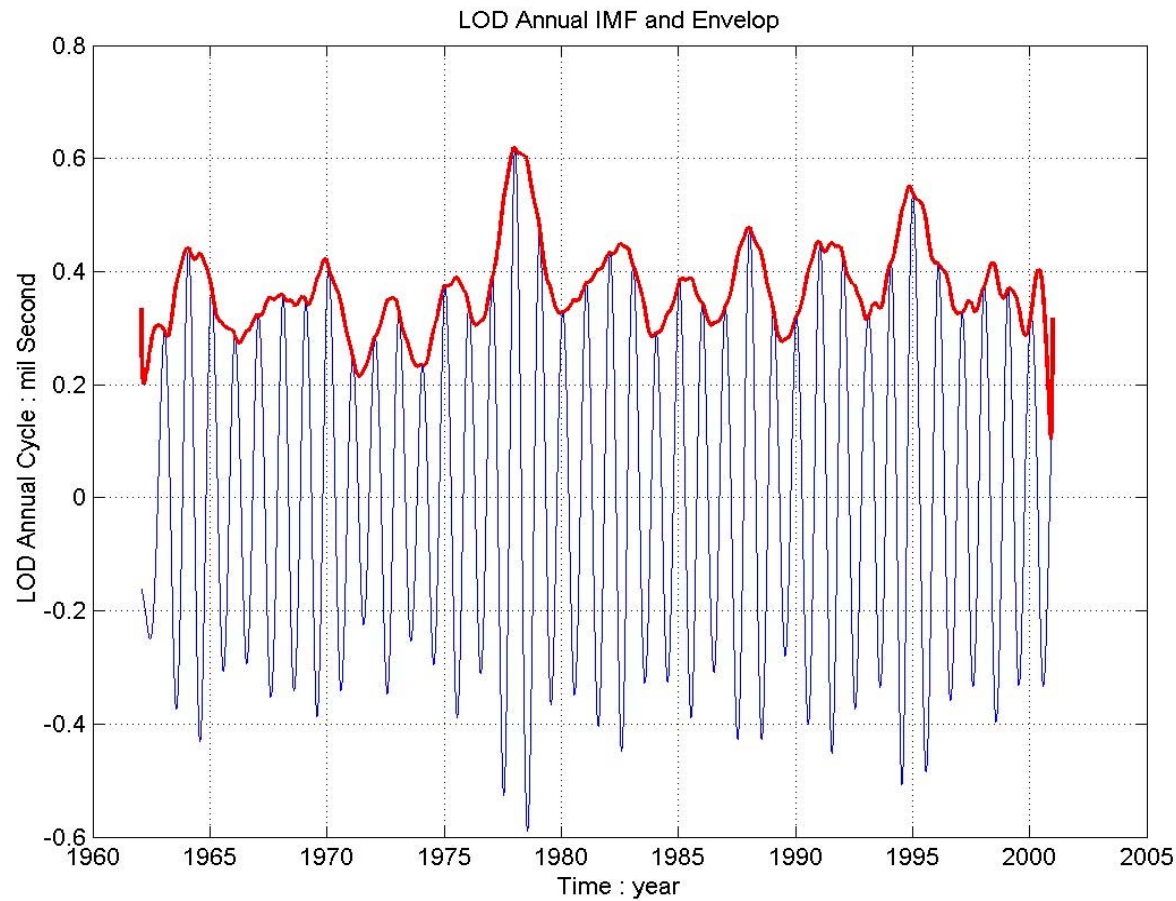


# Traditional View

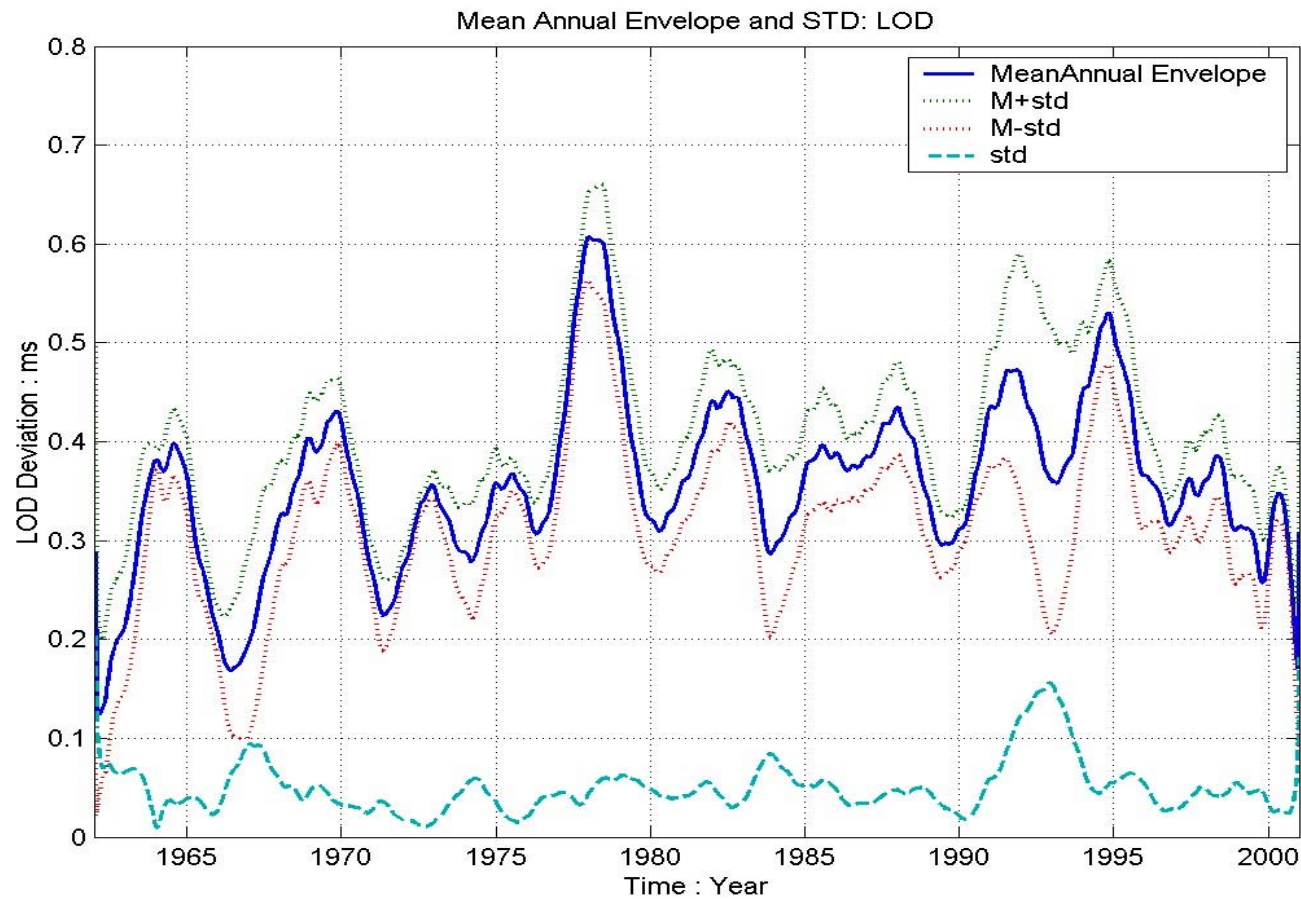
*a la Hahn (1995) : Hilbert*



# LOD : Mean envelop from 11 different siftings



# Mean Envelopes for Annual Cycle IMFs





# Comparisons

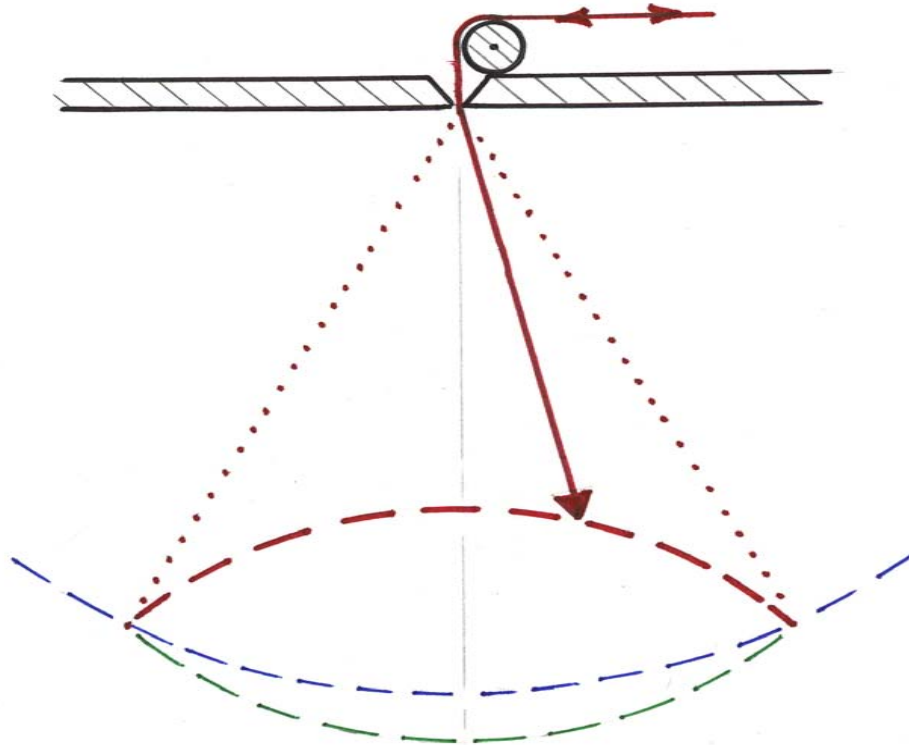
	<b>Fourier</b>	<b>Wavelet</b>	<b>Hilbert</b>
<b>Basis</b>	a priori	a priori	Adaptive
<b>Frequency</b>	Convolution: Global	Convolution: Regional	Differentiation: Local
<b>Presentation</b>	Energy- frequency	Energy-time- frequency	Energy-time- frequency
<b>Nonlinear</b>	no	no	yes
<b>Non-stationary</b>	no	yes	yes
<b>Feature extraction</b>	no	discrete : no continuous: yes	yes

# Characteristics of Data from Nonlinear Processes



A horizontal line with a colorful, noisy pattern in the center, flanked by two short horizontal yellow bars below it.

# Duffing Pendulum



$$\frac{d^2 x}{dt^2} + x + \varepsilon x^3 = a \cos \gamma t$$

$$\frac{d^2 x}{dt^2} + x(1 + \varepsilon x^2) = a \cos \gamma t$$

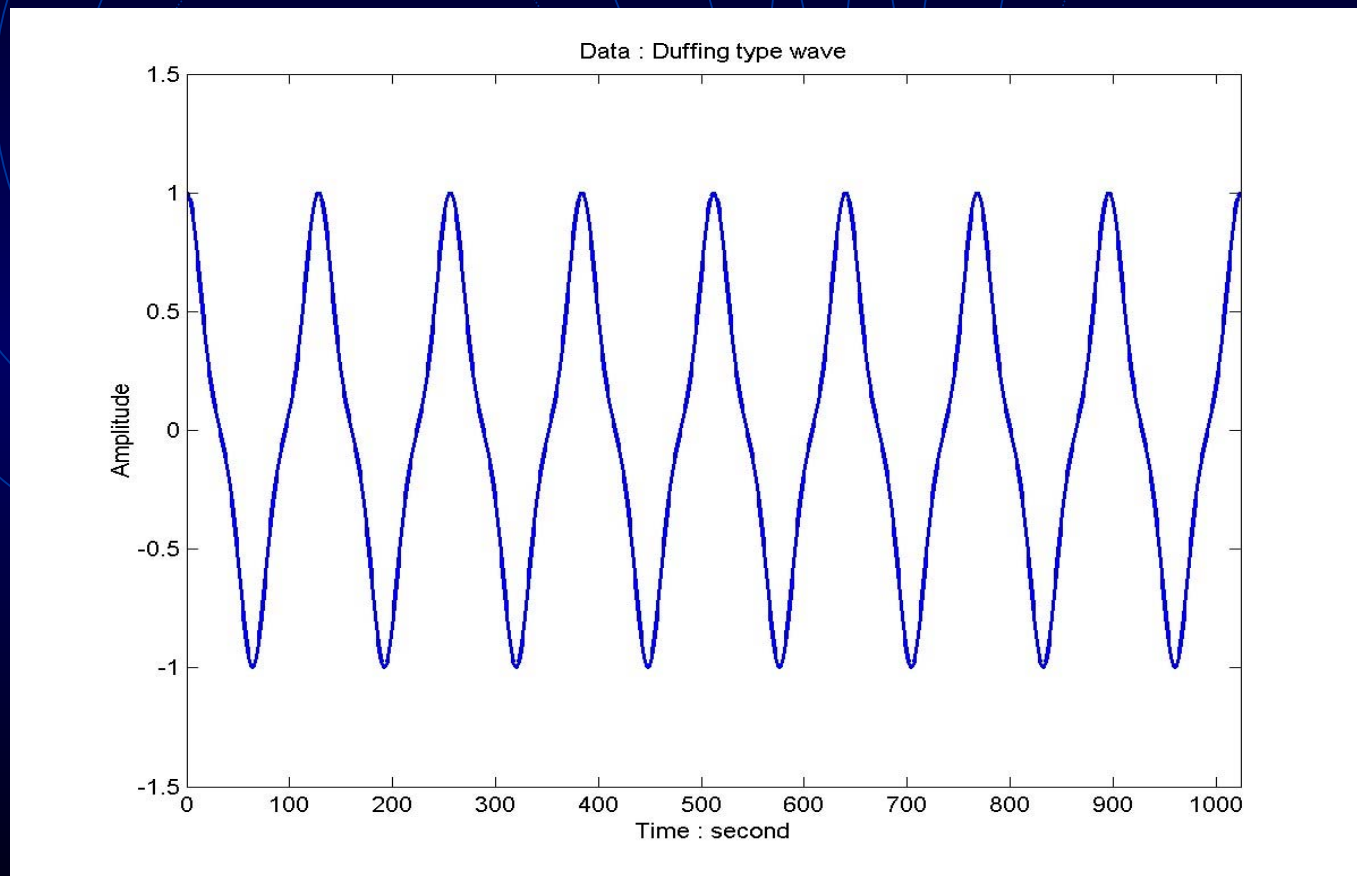


The background is a dark blue gradient. Overlaid on this are three sets of concentric circles in a lighter blue color. One set is on the left, one is on the right, and one is at the bottom center. The circles are thin and do not have a solid fill.

# Hilbert's View on Nonlinear Data

# Duffing Type Wave

Data:  $x = \cos(\omega t + 0.3 \sin 2\omega t)$



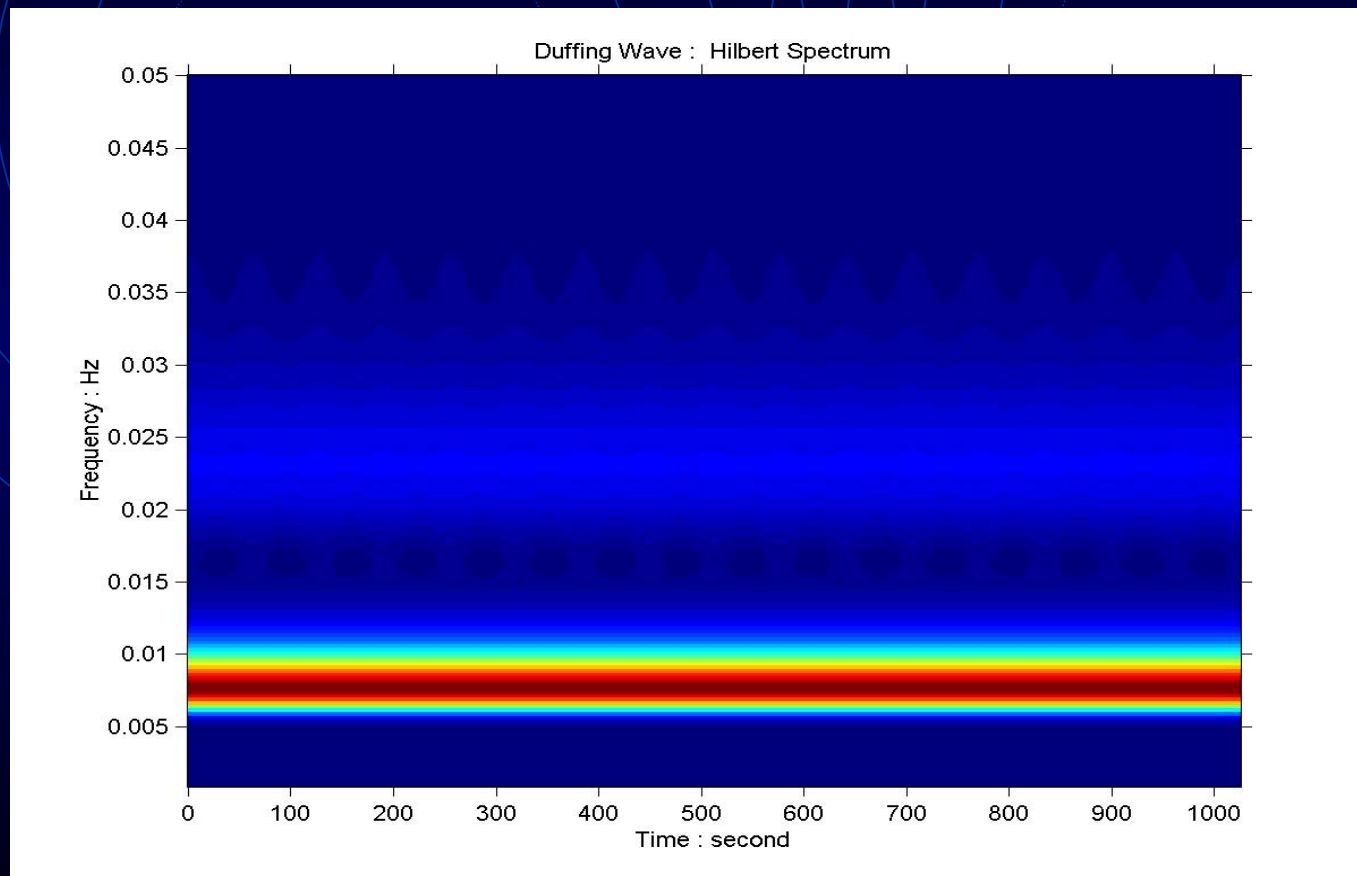
# Duffing Type Wave

## Perturbation Expansion



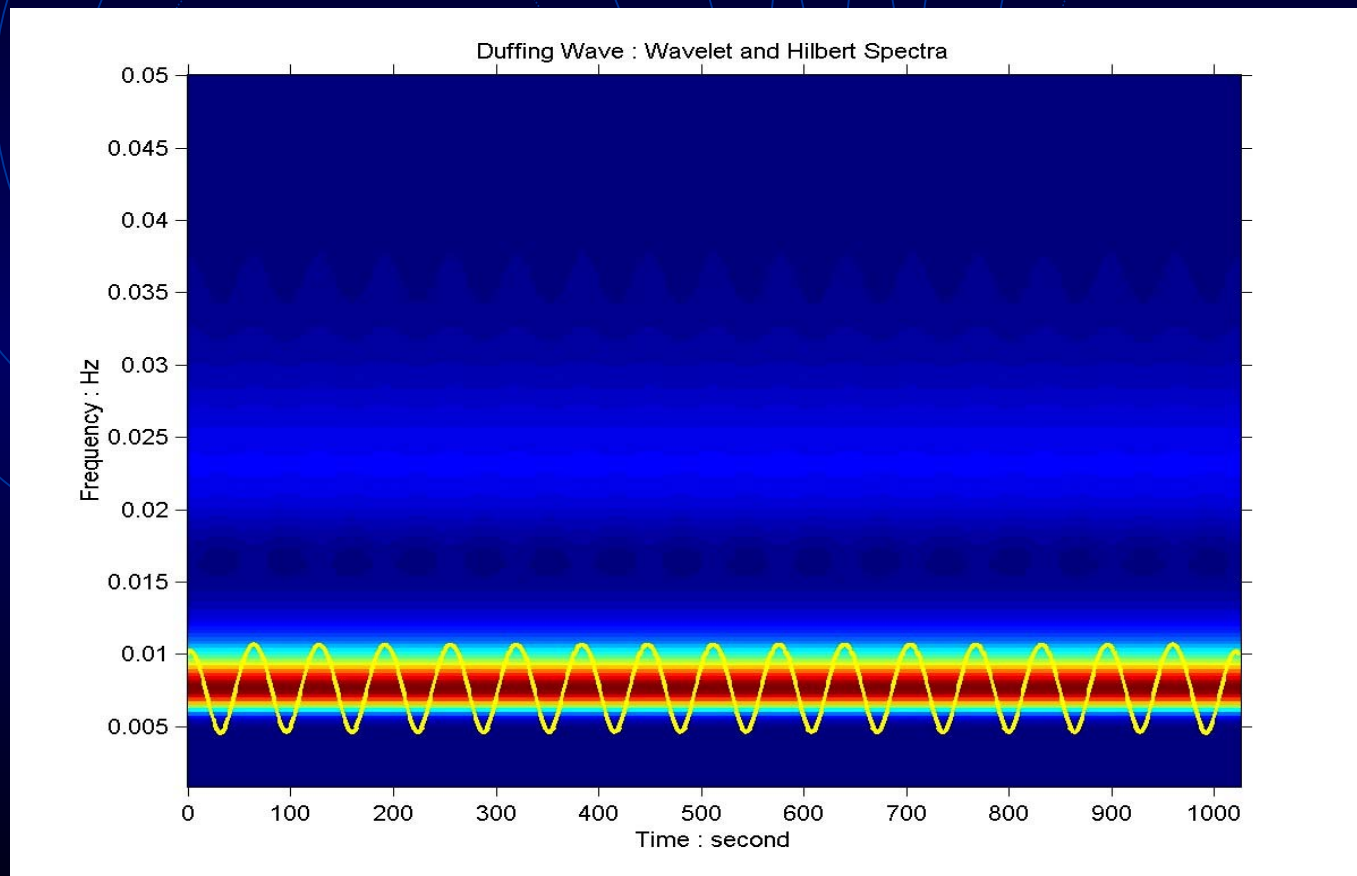
# Duffing Type Wave

## Wavelet Spectrum



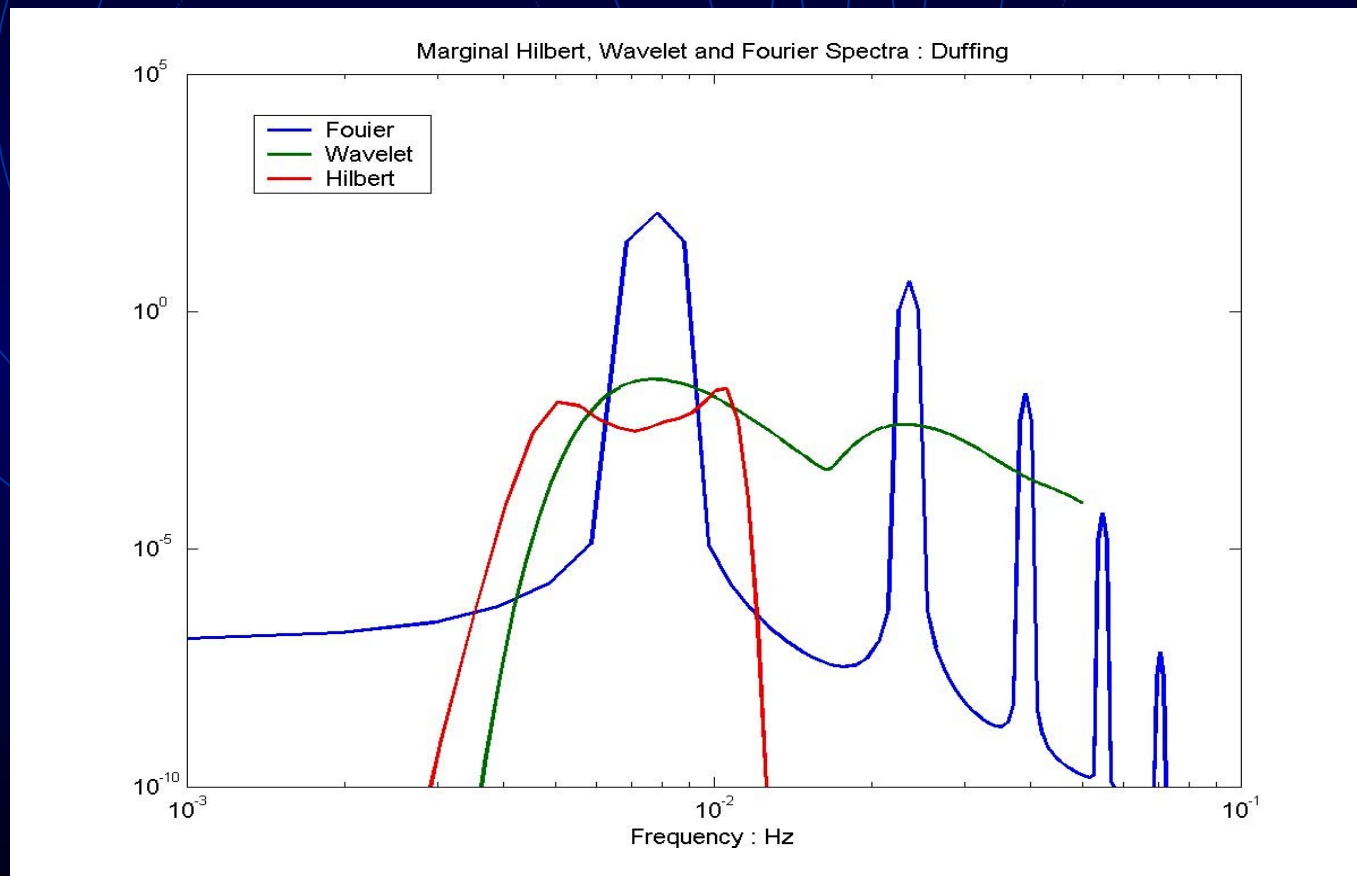
# Duffing Type Wave

## Hilbert Spectrum



# Duffing Type Wave

## Marginal Spectra



# Technology Description

## **Results:**

- **An adaptive basis to filter signal**
- **Frequency defined as a function of time by differentiation rather than convolution analysis**
- **Sharp identification of embedded structures**
- **A more simple and revealing interpretation than prior methods**

# **Market Potential**

## **Key Considerations**

- **Conceptually simple and direct**
- **An efficient, adaptive, user-friendly set of algorithms**
- **Capable of analyzing nonlinear and nonstationary signals**
- **Improves accuracy by using an adaptive basis to preserve intrinsic properties of data**
- **Yields results with more physical meaning and a different perspective than existing tools**
- **Useful in analyzing a variety of from nonlinear and nonstationary processes**



# Possible Applications


- Vibration, **speech and acoustic signal analyses** : this also applies to **machine health monitoring**.
- Non-destructive test and structural Health monitoring
- Earthquake Engineering
- As a nonlinear Filter
- **Bio-medical applications**
- Time-Frequency-Energy distribution for general nonlinear and nonstationary data analysis, for example, turbulence

## Sound Enhancement :

- Fourier filter is linear and stationary; it works in Frequency domain
- Fourier filter will take away harmonics and dull the sharp corners of all the fundamentals
- EMD filter is nonlinear and intermittent; it works in Time domain
- EMD filter will take the unwanted noise of short periods and leaves the fundamentals unchanged

# EMD as Filter

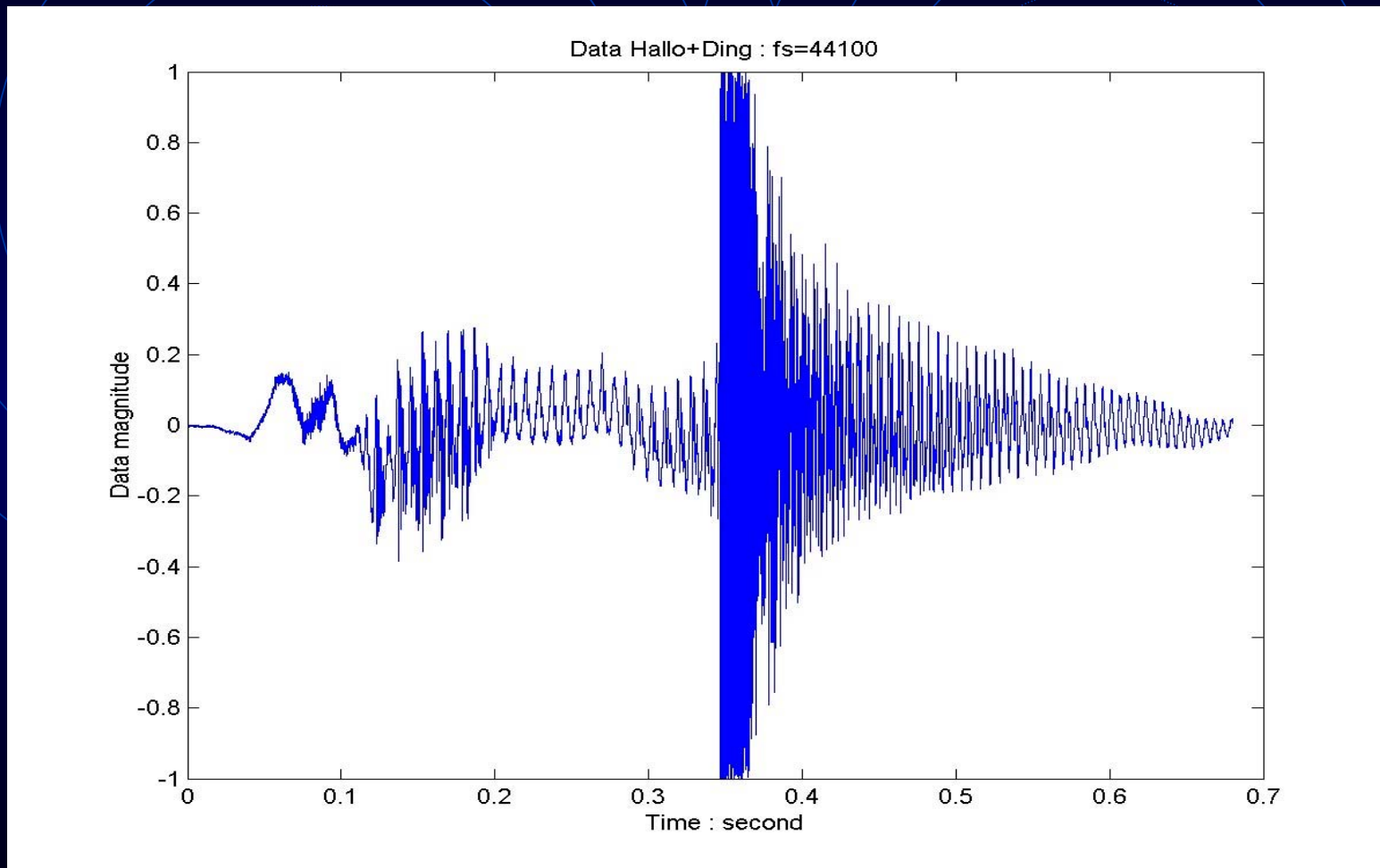
EMD as Filter

The background is a dark blue gradient. It features a pattern of concentric circles in a lighter blue color, centered around the text. Overlaid on these circles is a faint grid of dashed lines.

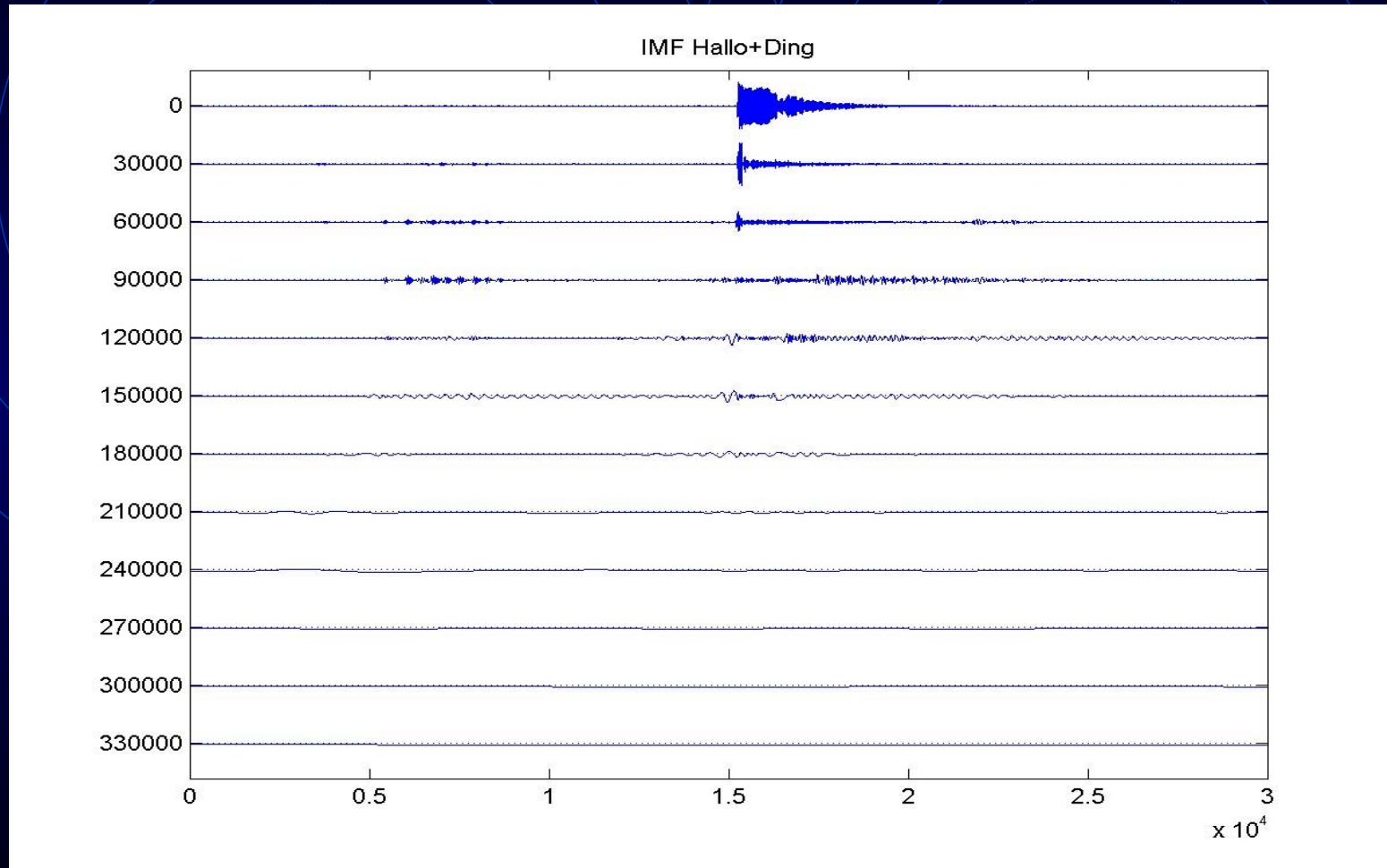
# An Example : Removal of Unwanted Sound

HHT Filtering to Separate  
Ding from Hello

# Data : Hallo + Ding



# IMF : Hallo + Ding

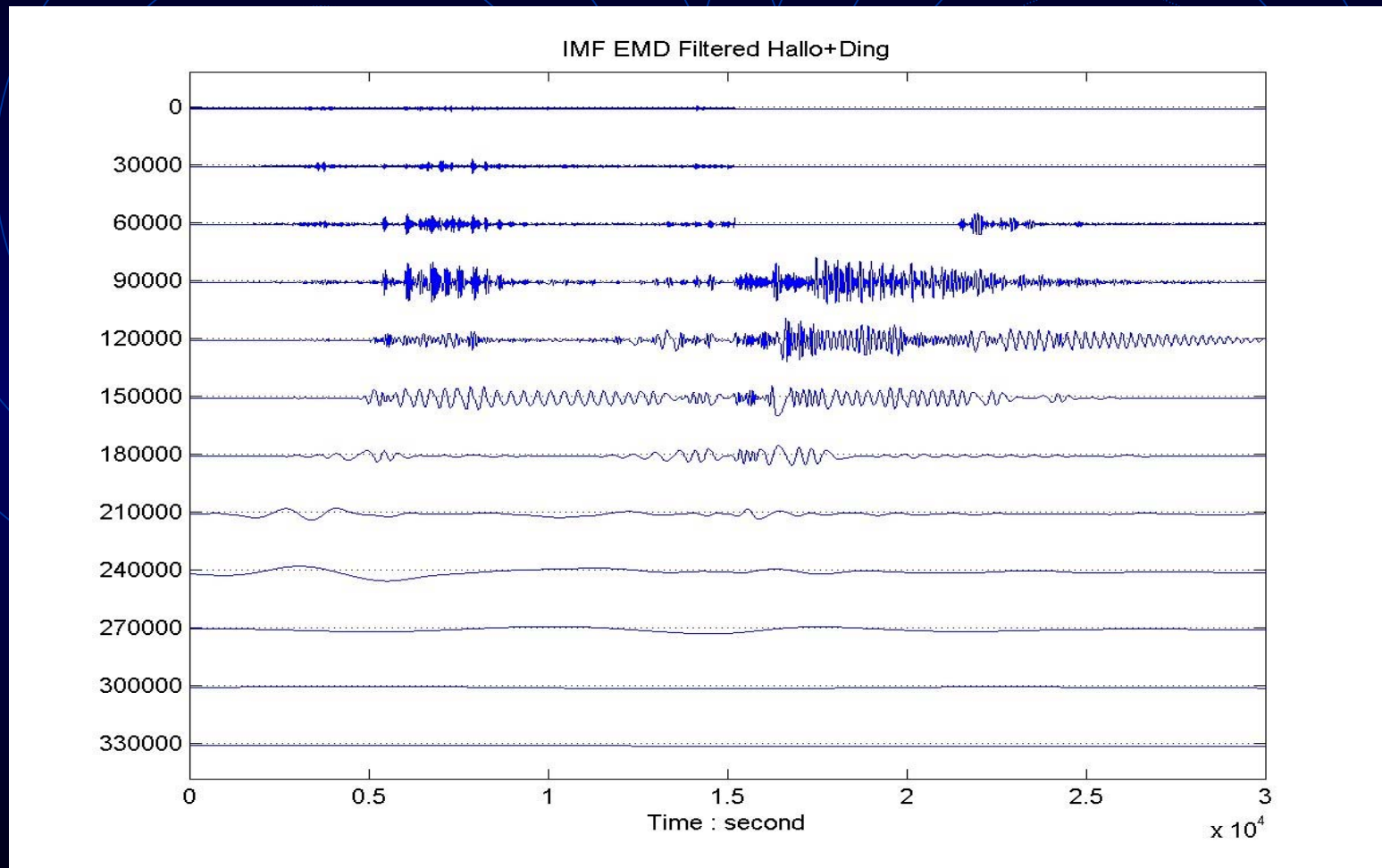


## Filter for Hallo + Ding is defined as

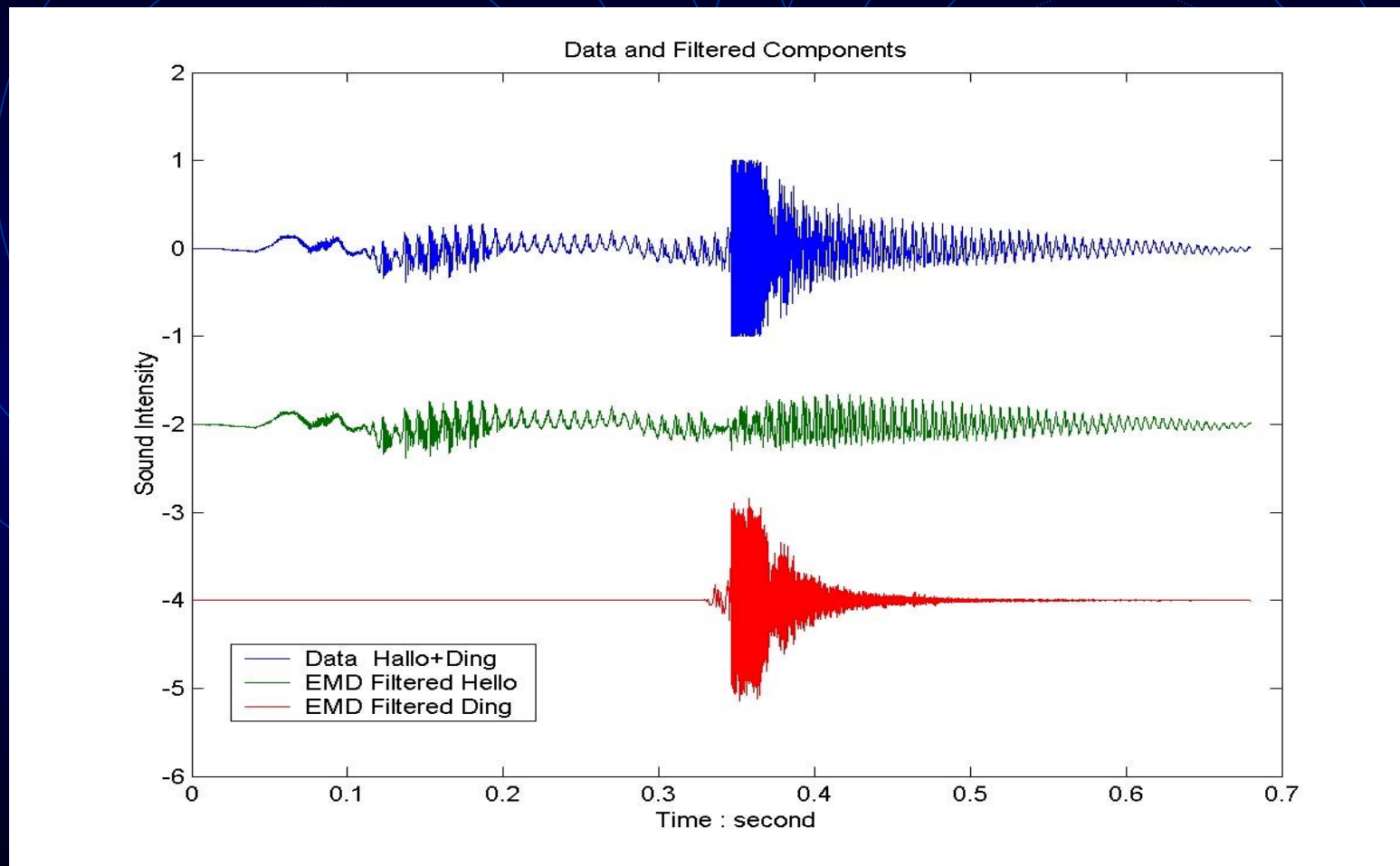
- $c1(15200:30000) = 0;$
- $c2(15200:30000) = 0;$
- $c3(15200:21400) = 0;$
- For  $c4$  to  $c9$  :  $q = [\cos(2\pi t/1200) + 1]/2$  ;  
for  $t=0:1200$ , centered at 15200.



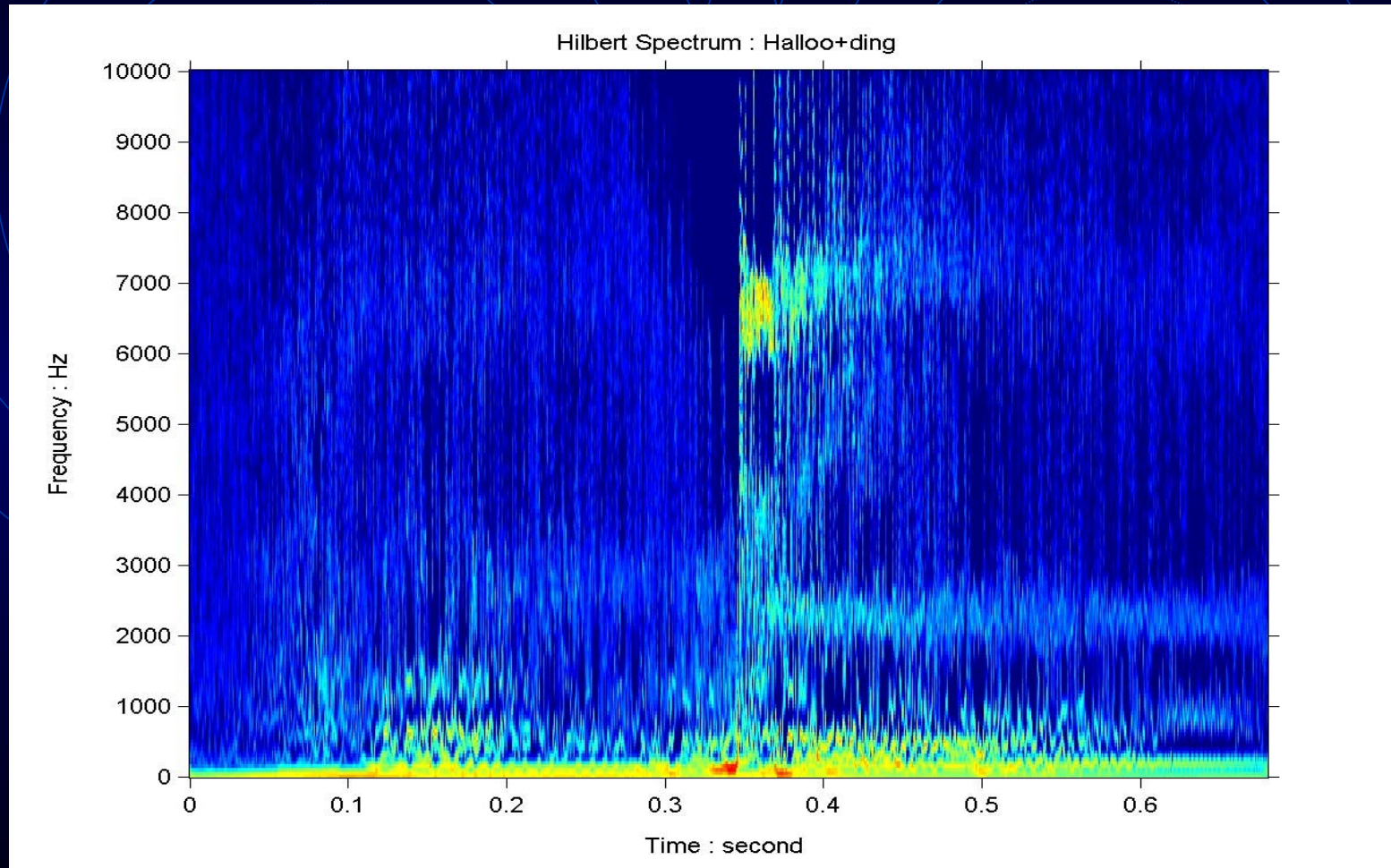
# IMF Filtered : Hallo



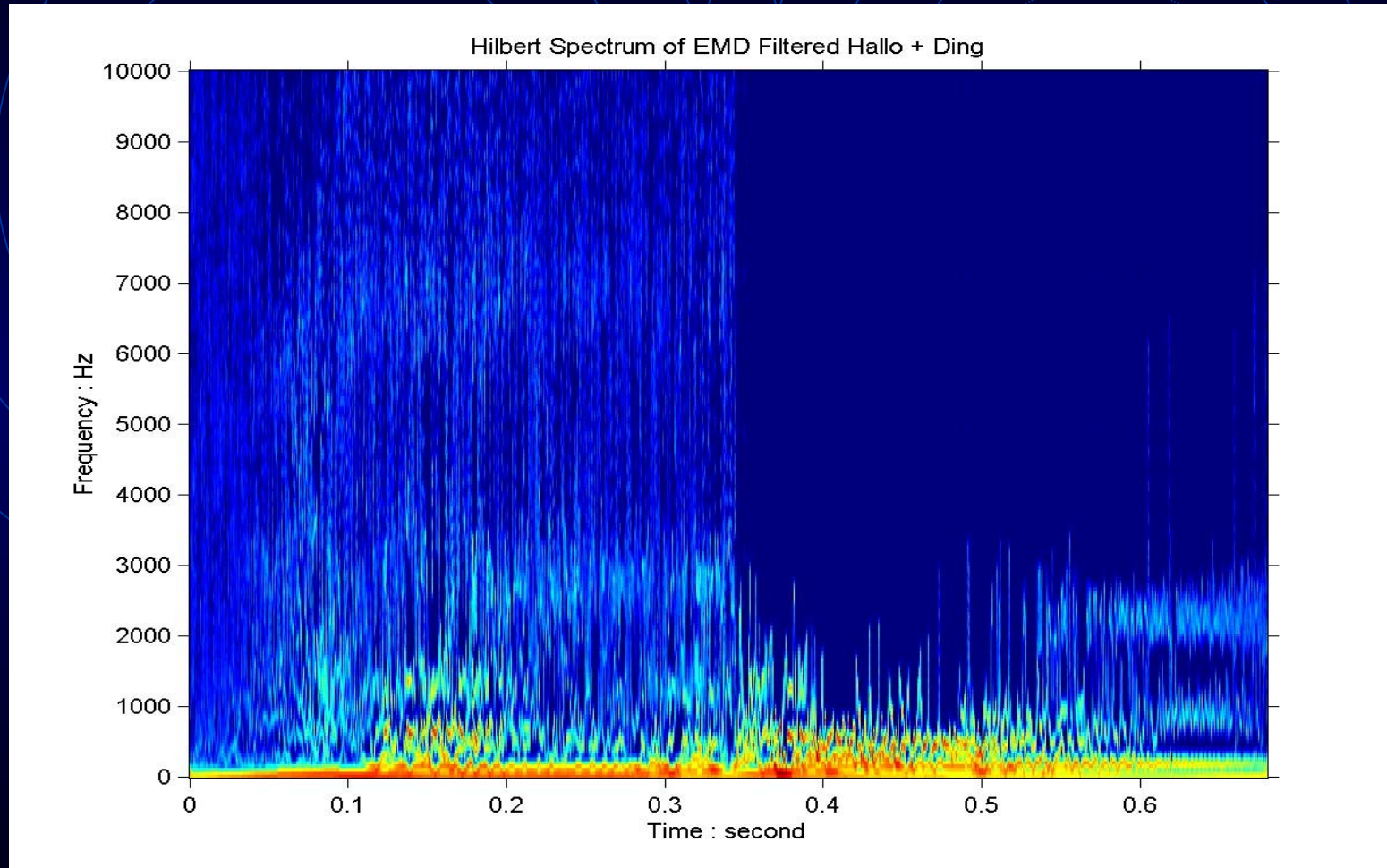
# Data and Filtered Components



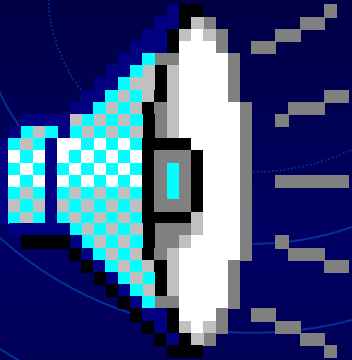
# Hilbert Spectrum : Hallo + Ding



# Hilbert Spectrum Filtered : Hallo



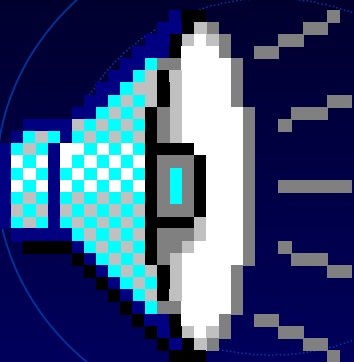
# Sound Effects : Data



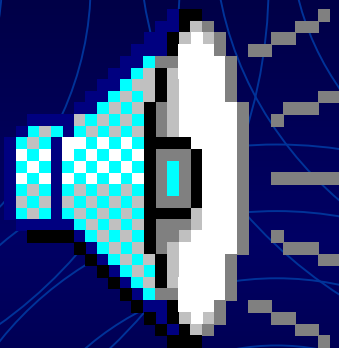
Raw data : Hallo + Ding



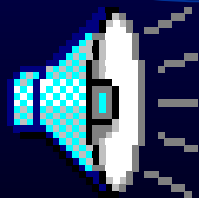
# Sound Effects : Fourier Filtered



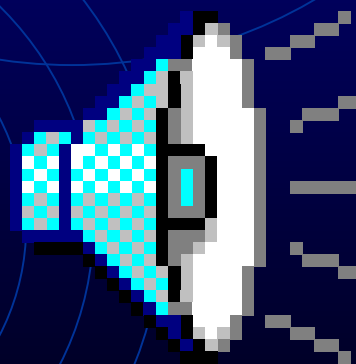
Fourier 3K



Fourier 2K

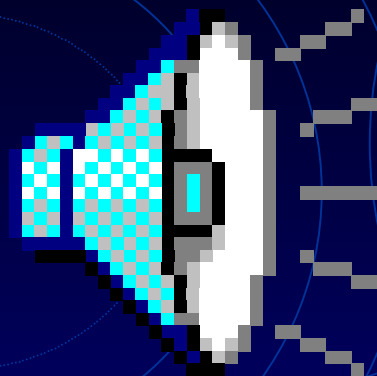


Original

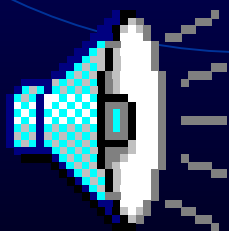


Fourier 1K

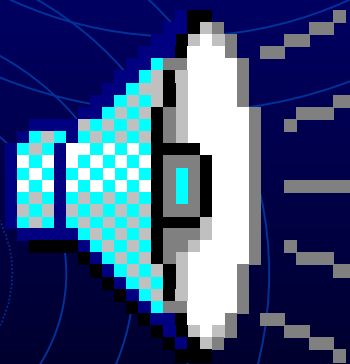
# Sound Effects : EMD Filtered



EMD Filtered Hello



Original Sound



EMD Filtered Ding

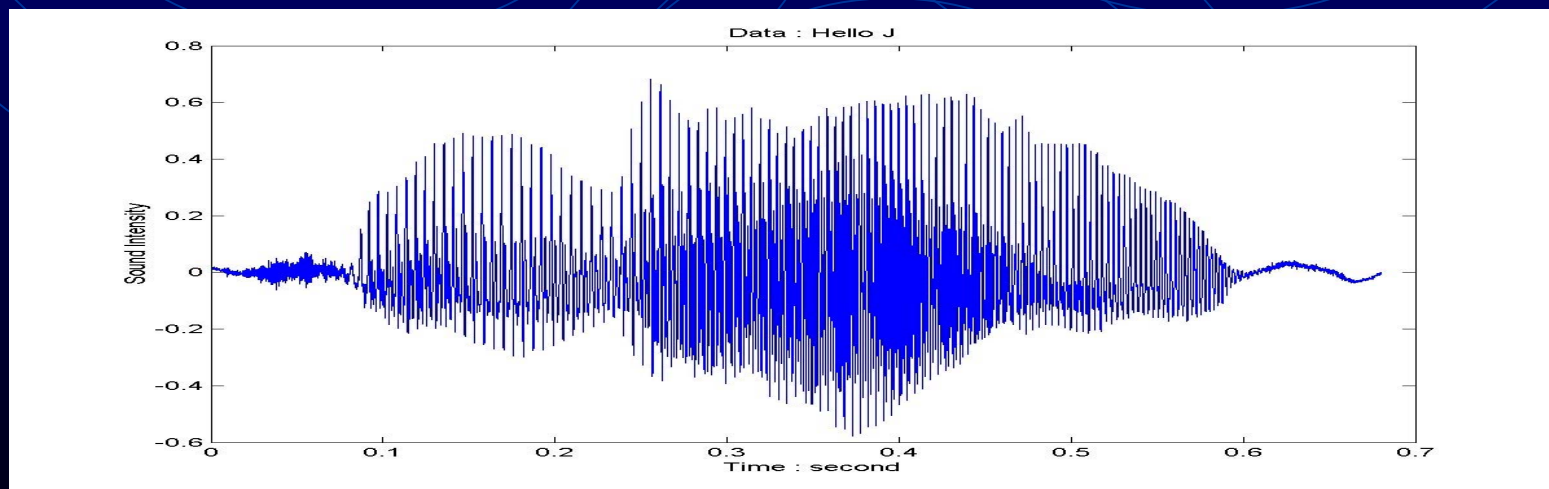
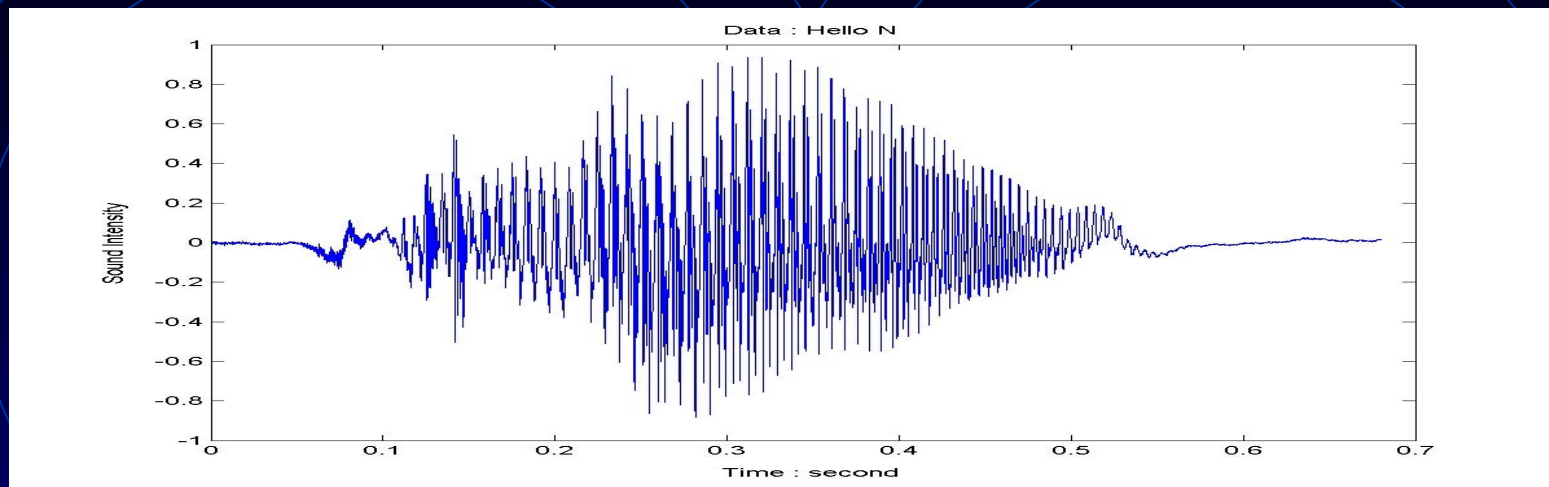


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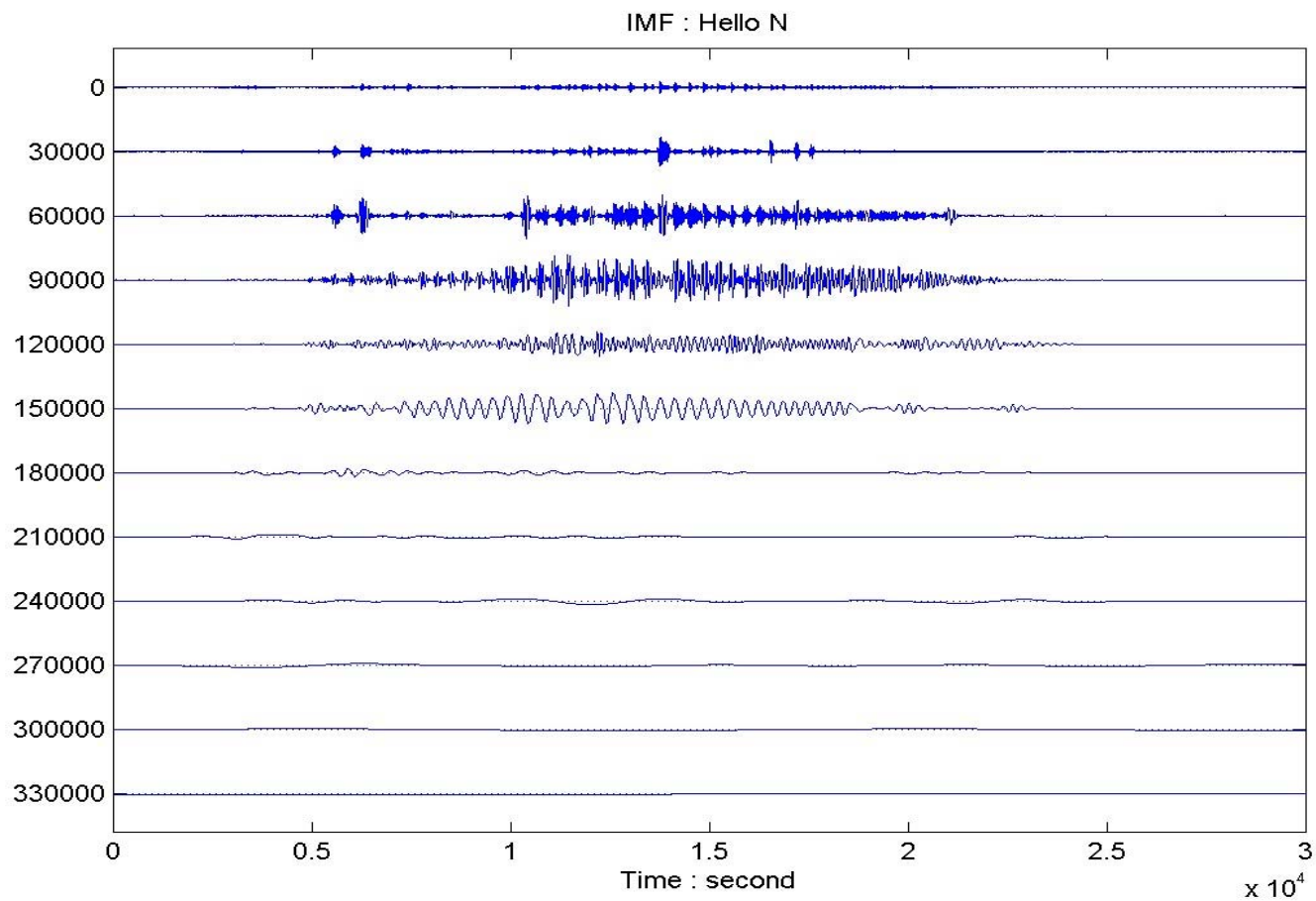
# Hilbert Spectra for Different Speakers

Potential Application for Speaker Identification

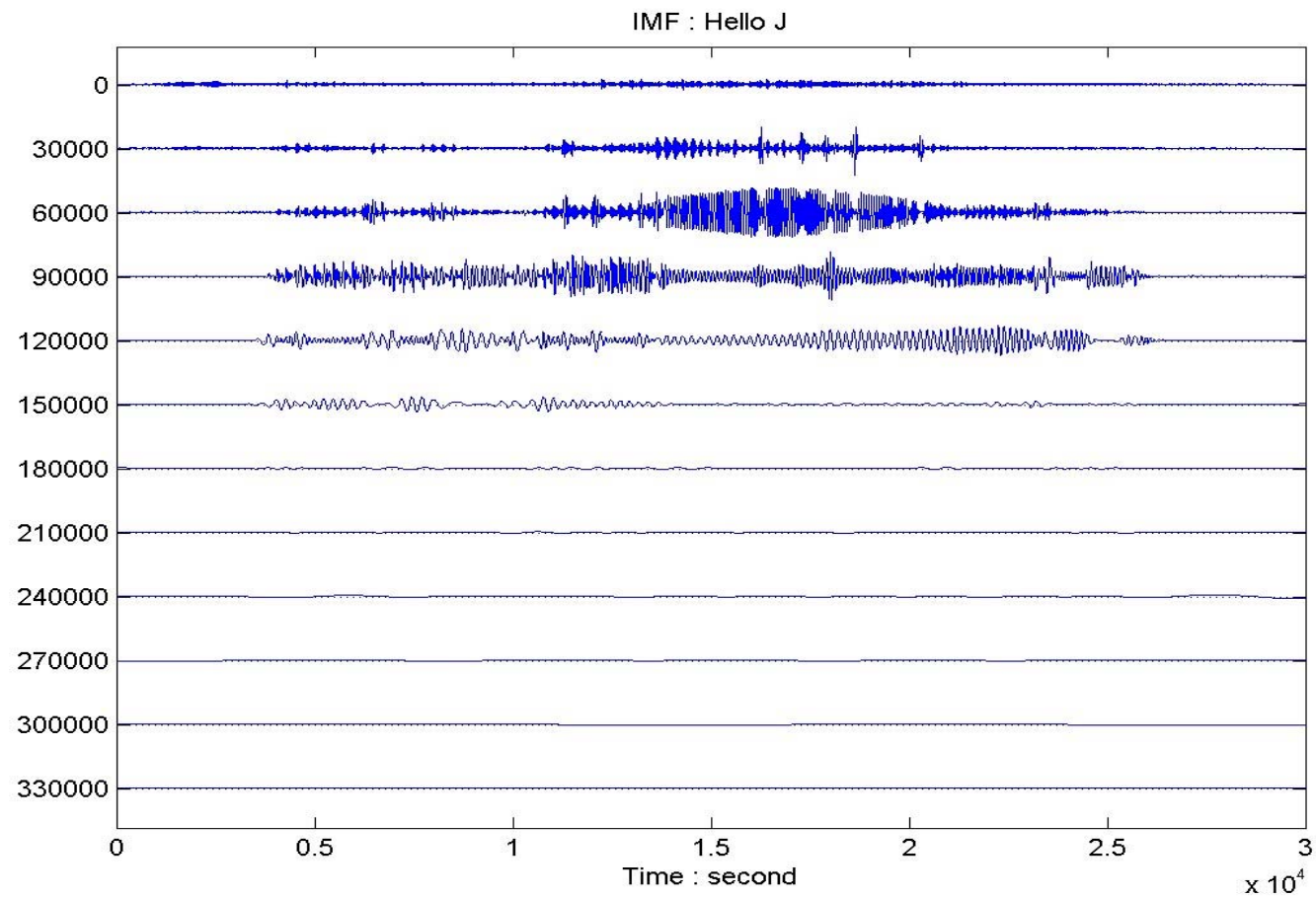
# Difference between Speakers



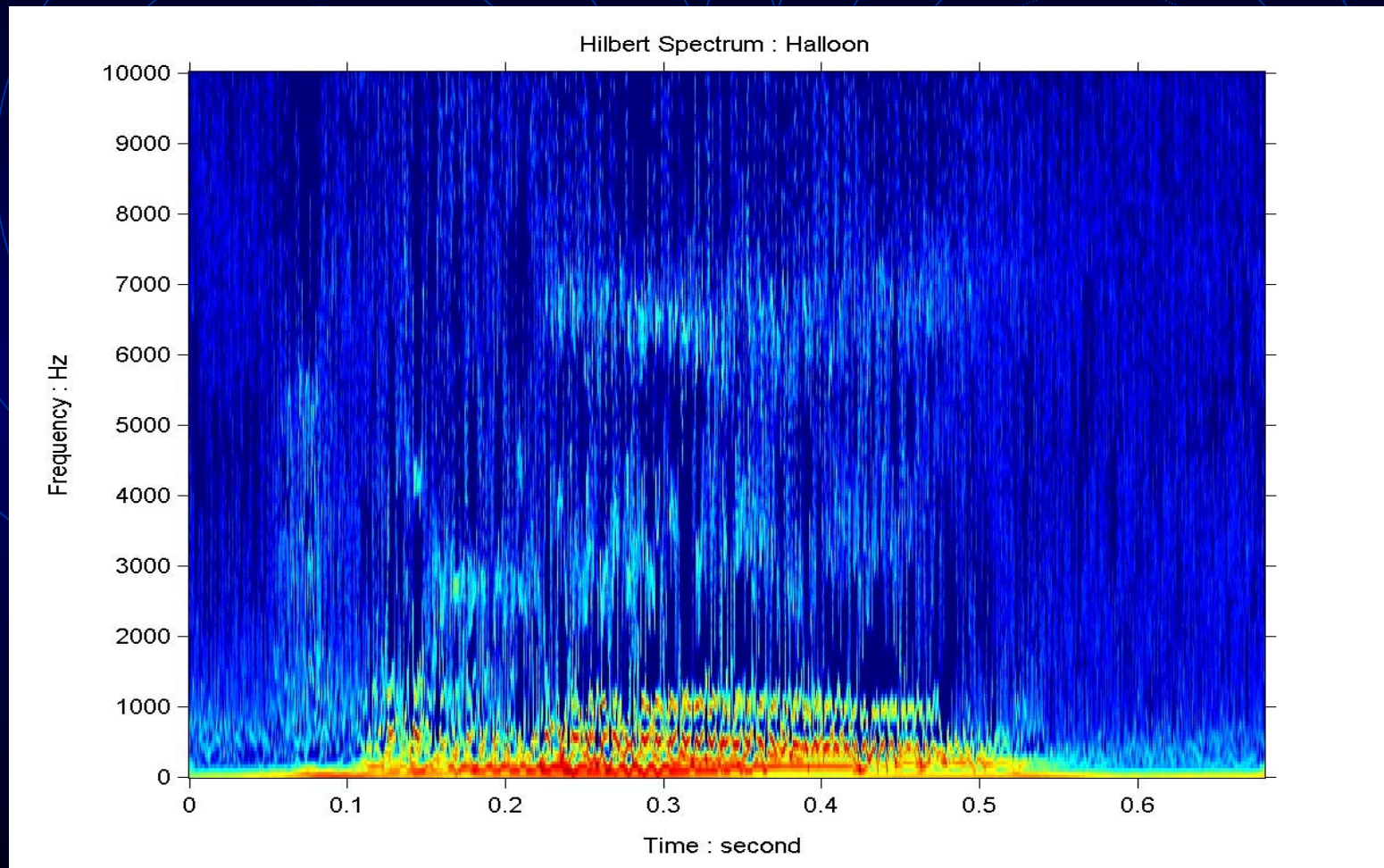
# IMF : Hello N



# IMF : Hello J

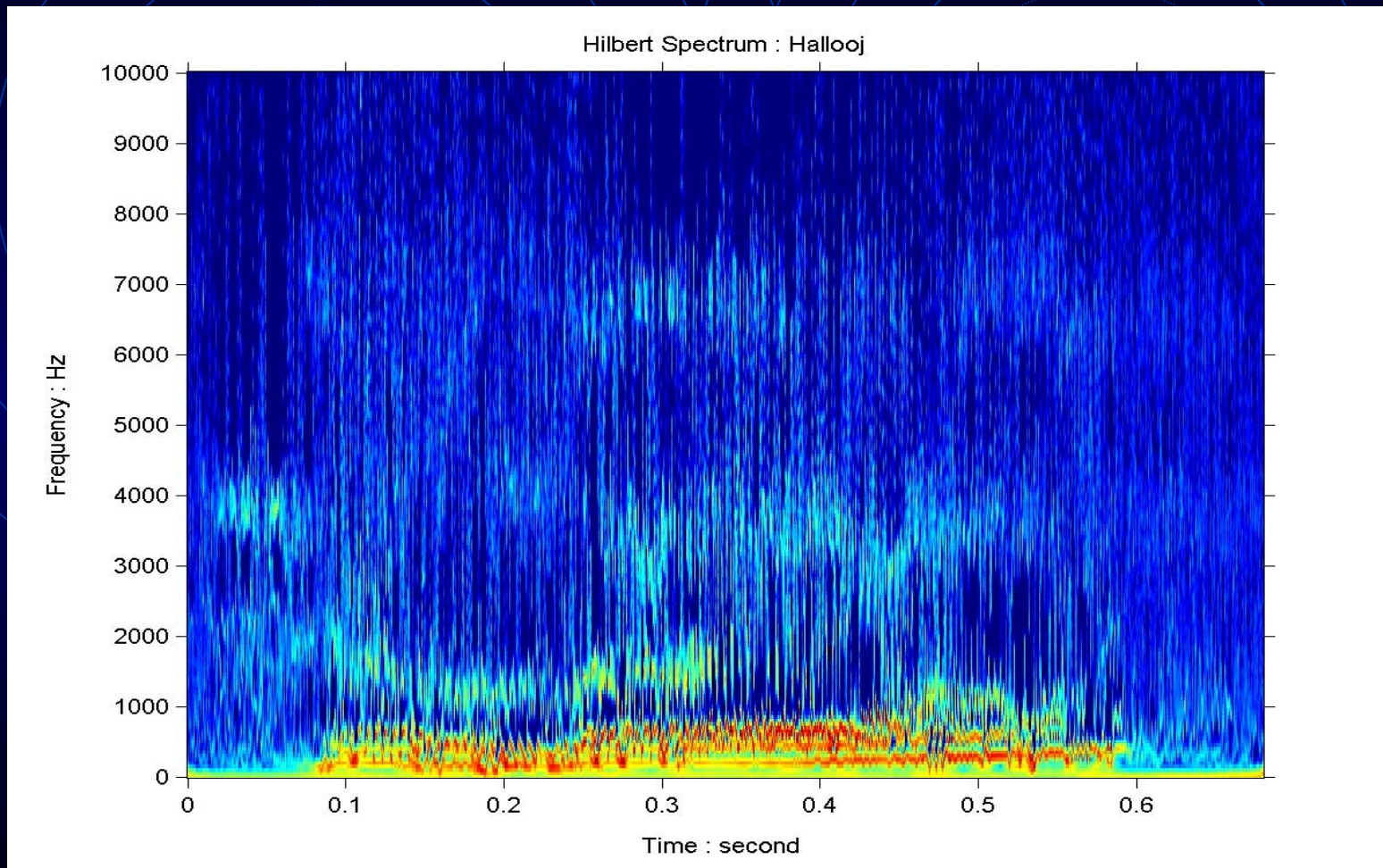


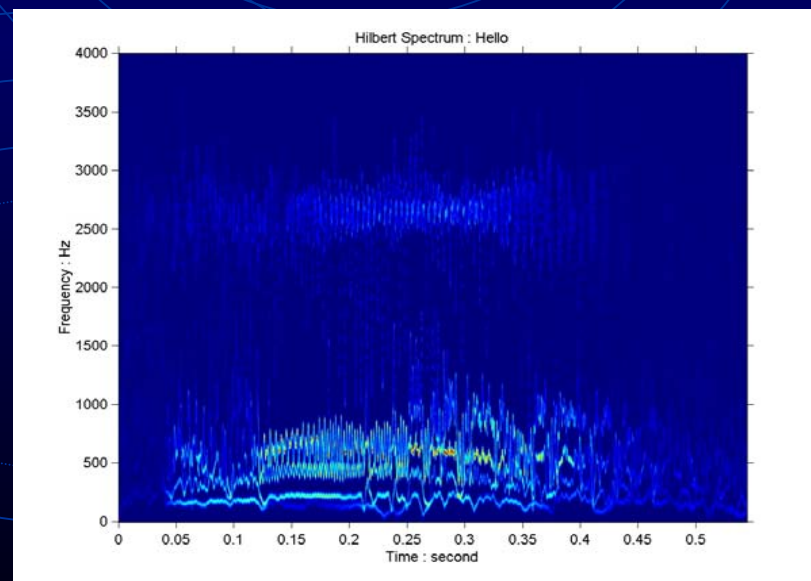
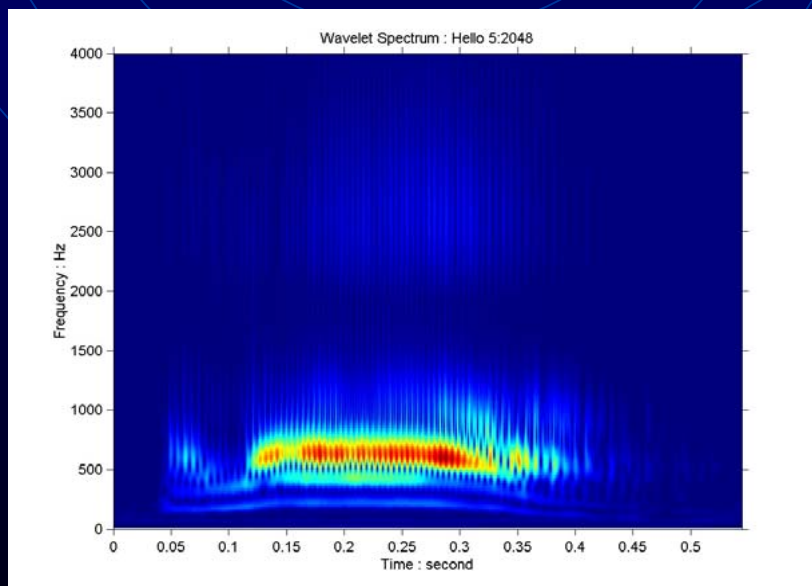
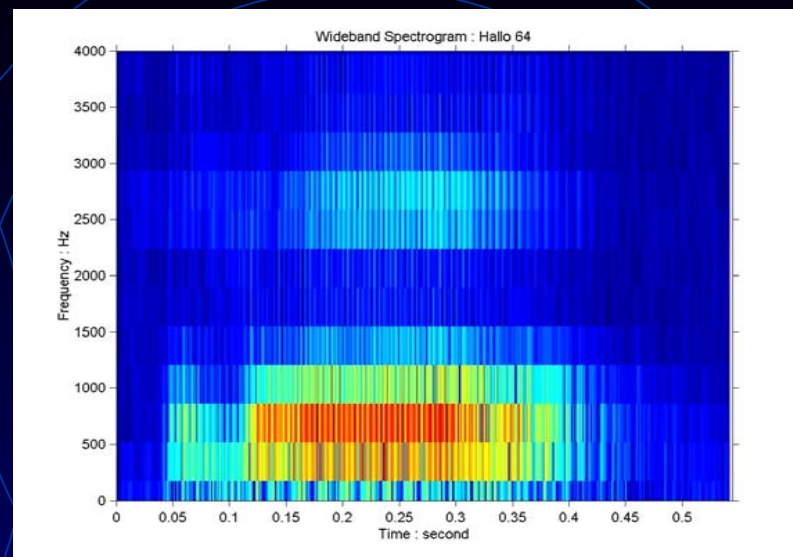
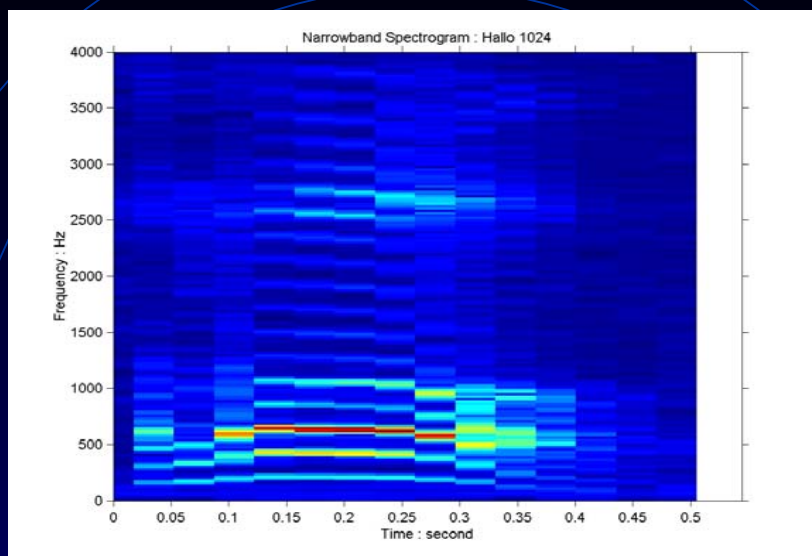
# Hilbert Spectrum : Hello N





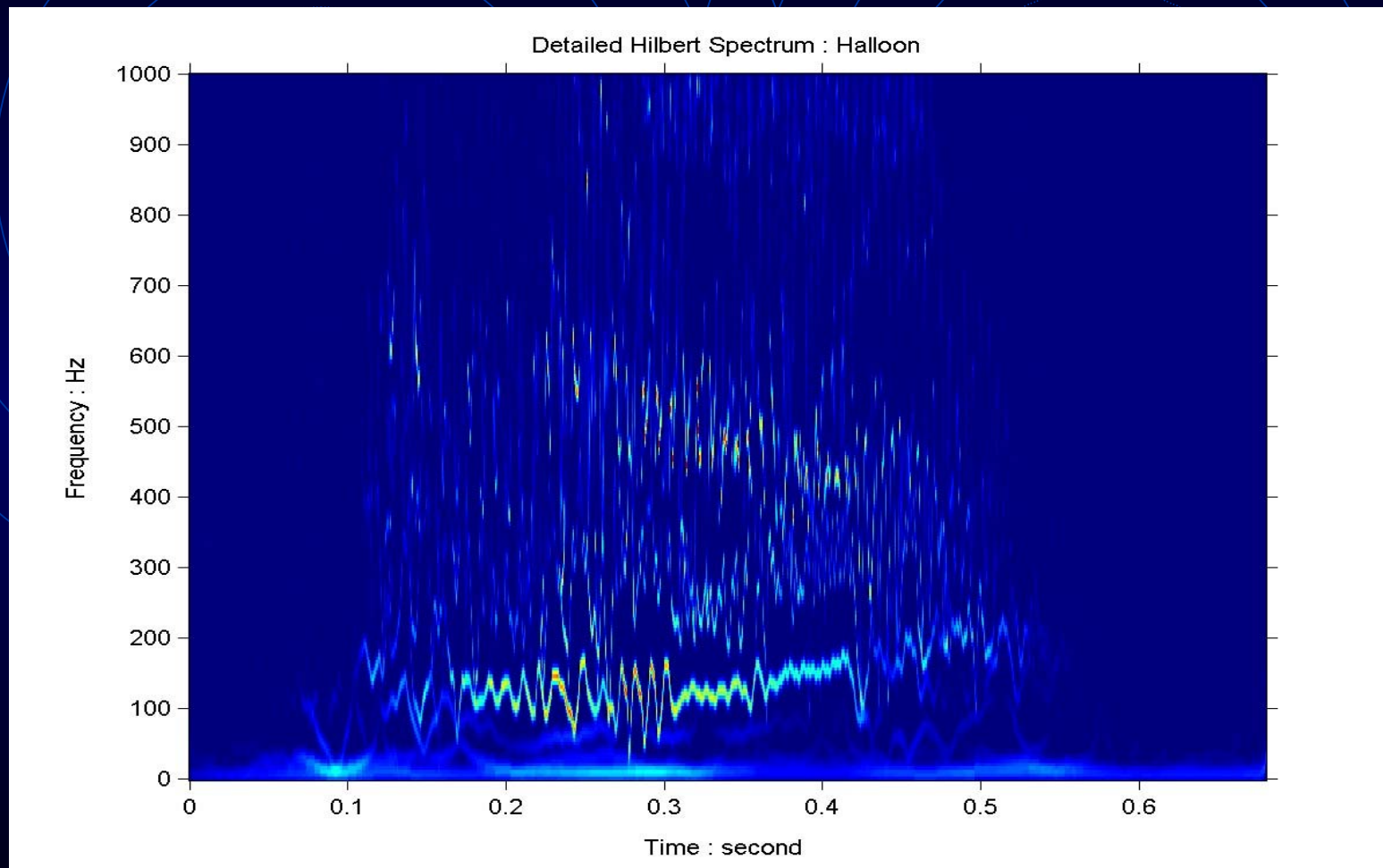
# Hilbert Spectrum : Hello J



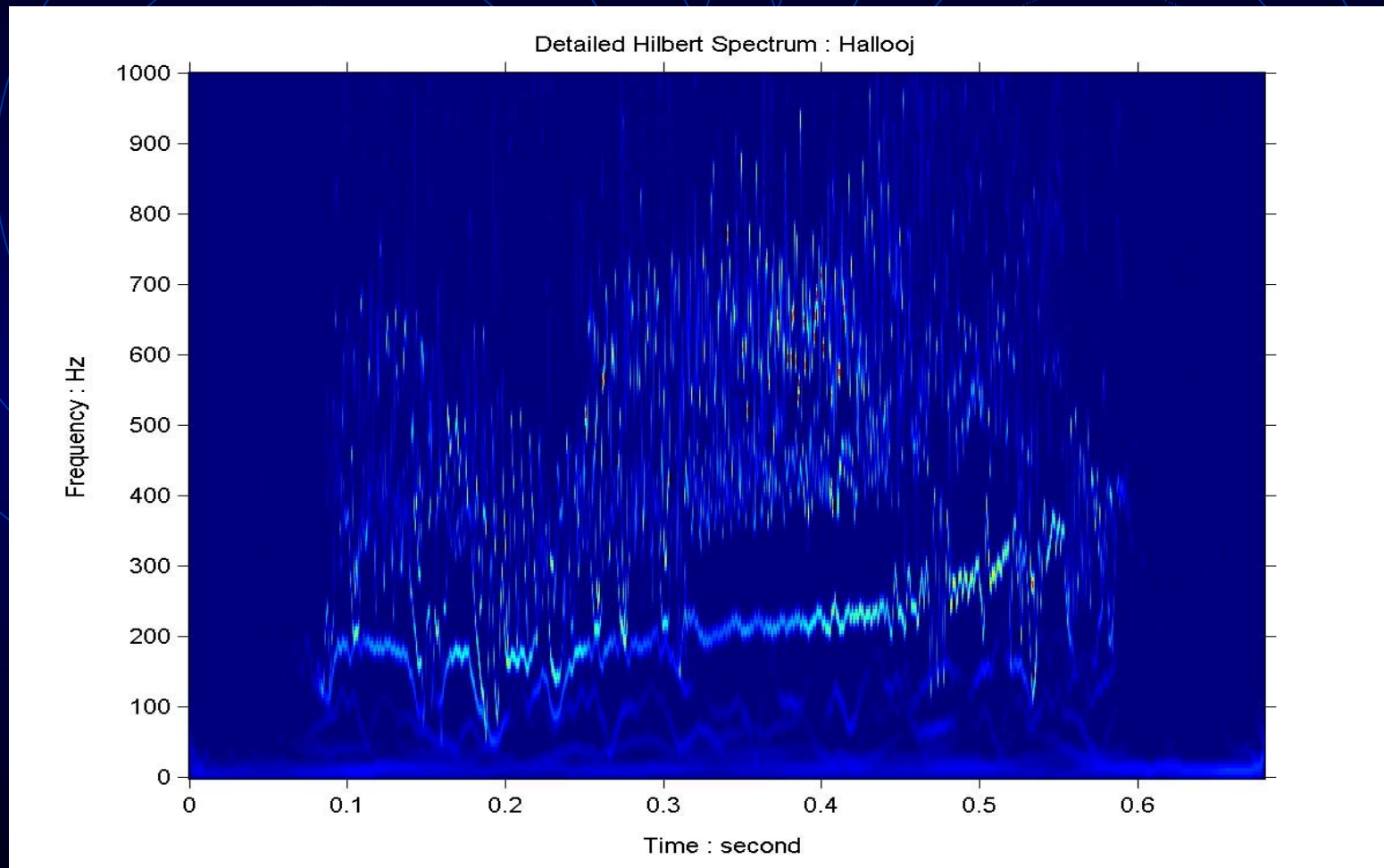




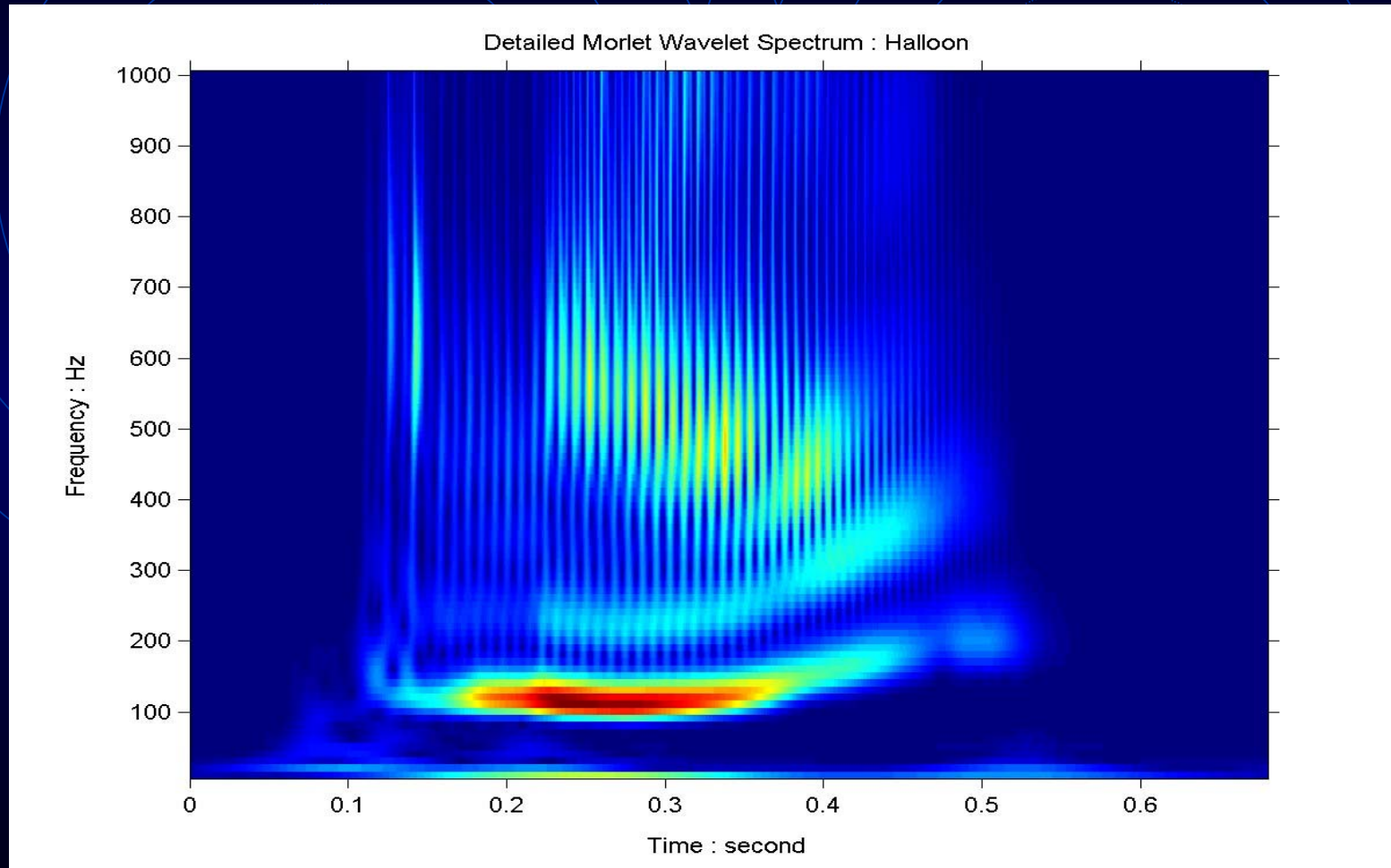
# Detailed Hilbert Spectrum : Hello N



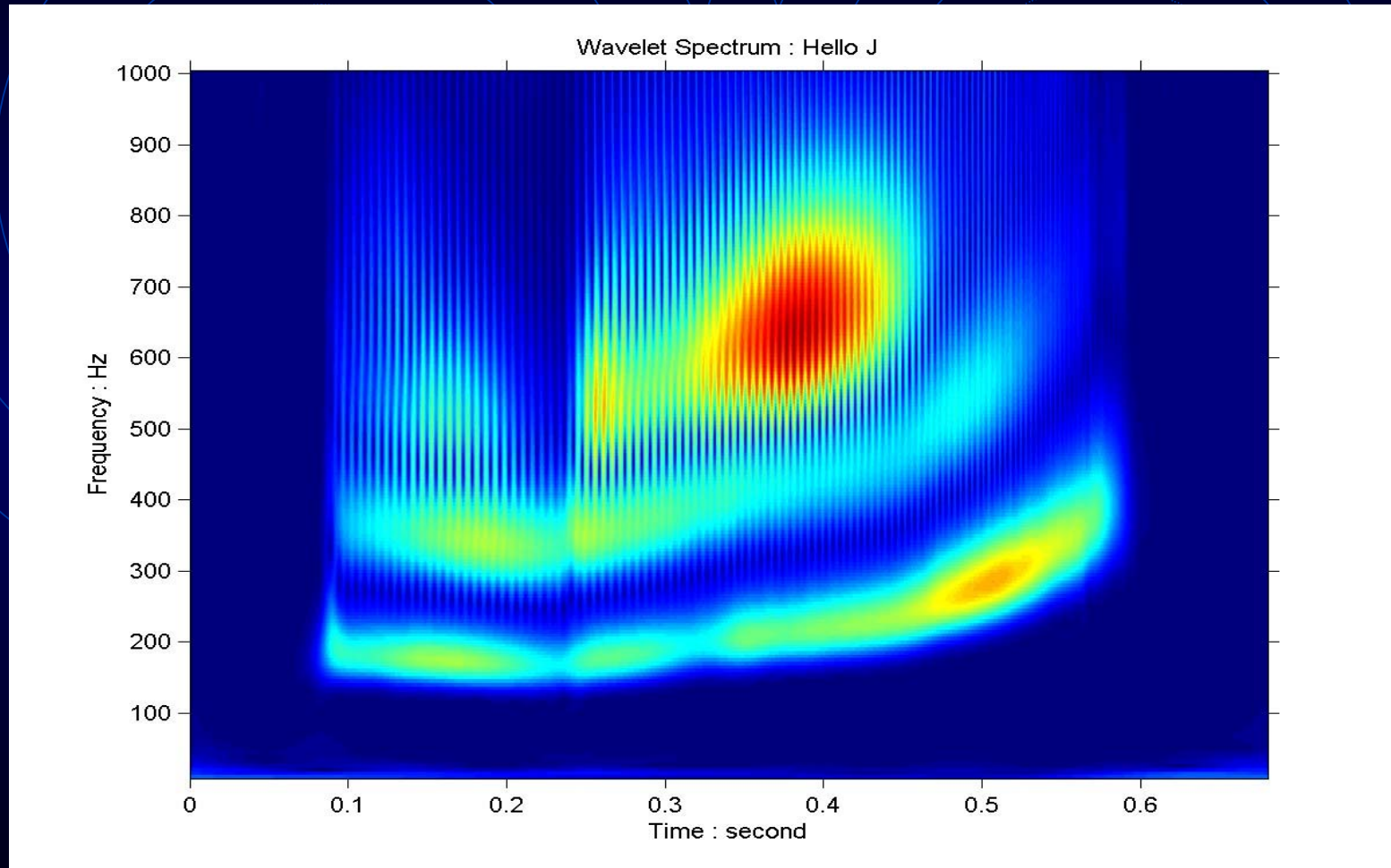
# Detailed Hilbert Spectrum : Hello J



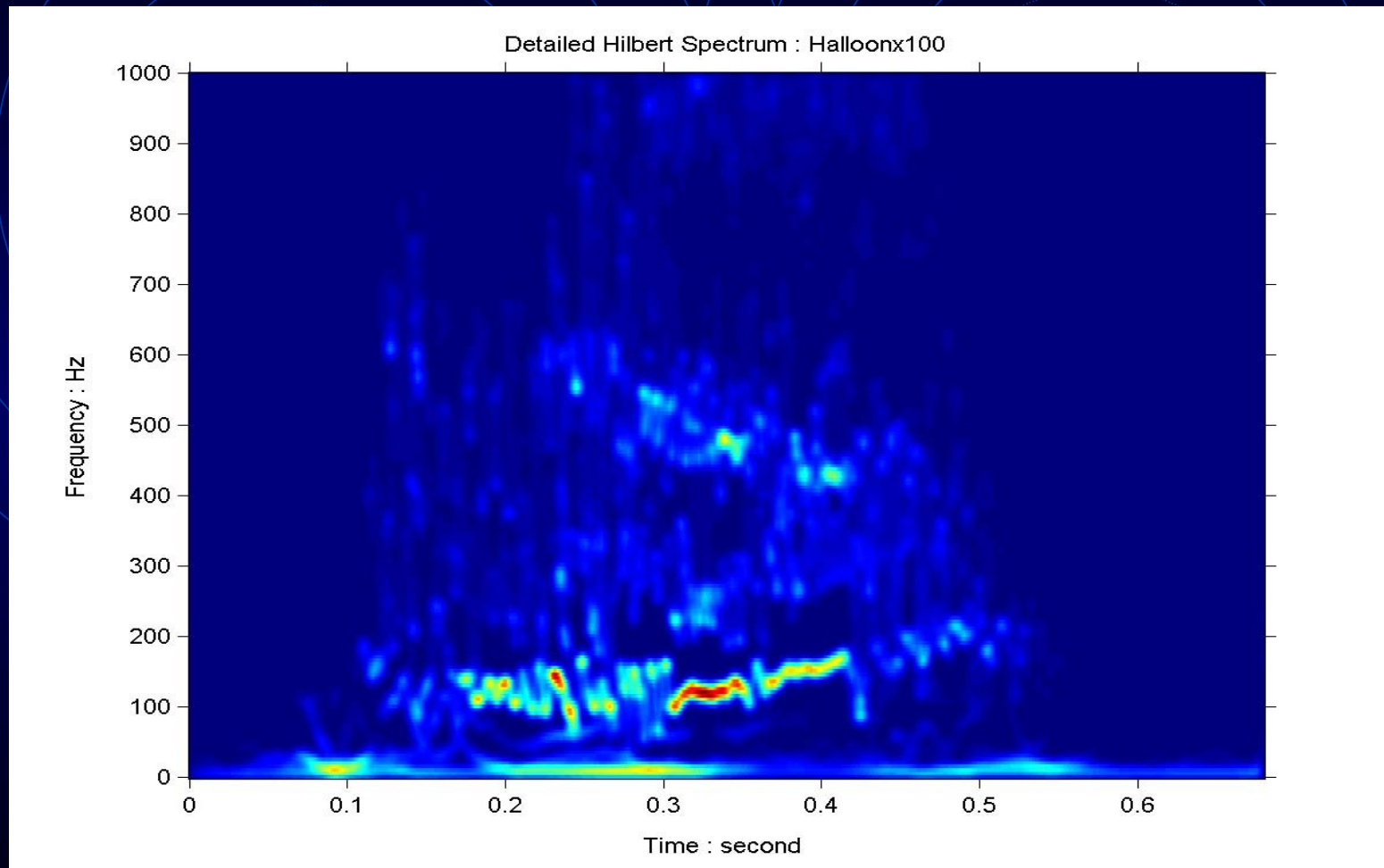
# Detailed Wavelet Spectrum : Hello N



# Detailed Wavelet Spectrum : Hello J

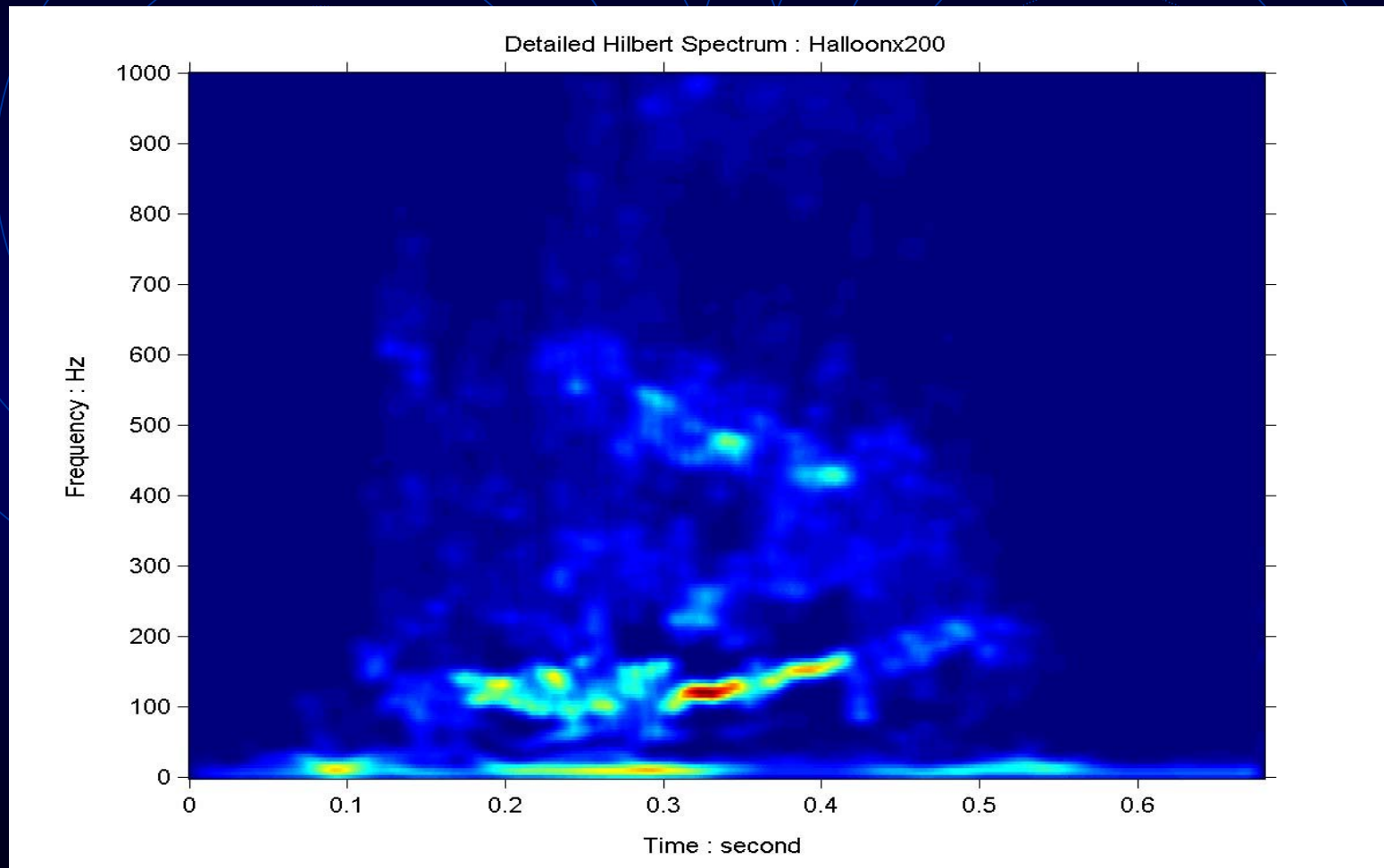


# 100 Smoothed H Spectrum : Hello N





# 200 Smoothed H Spectrum : Hello N

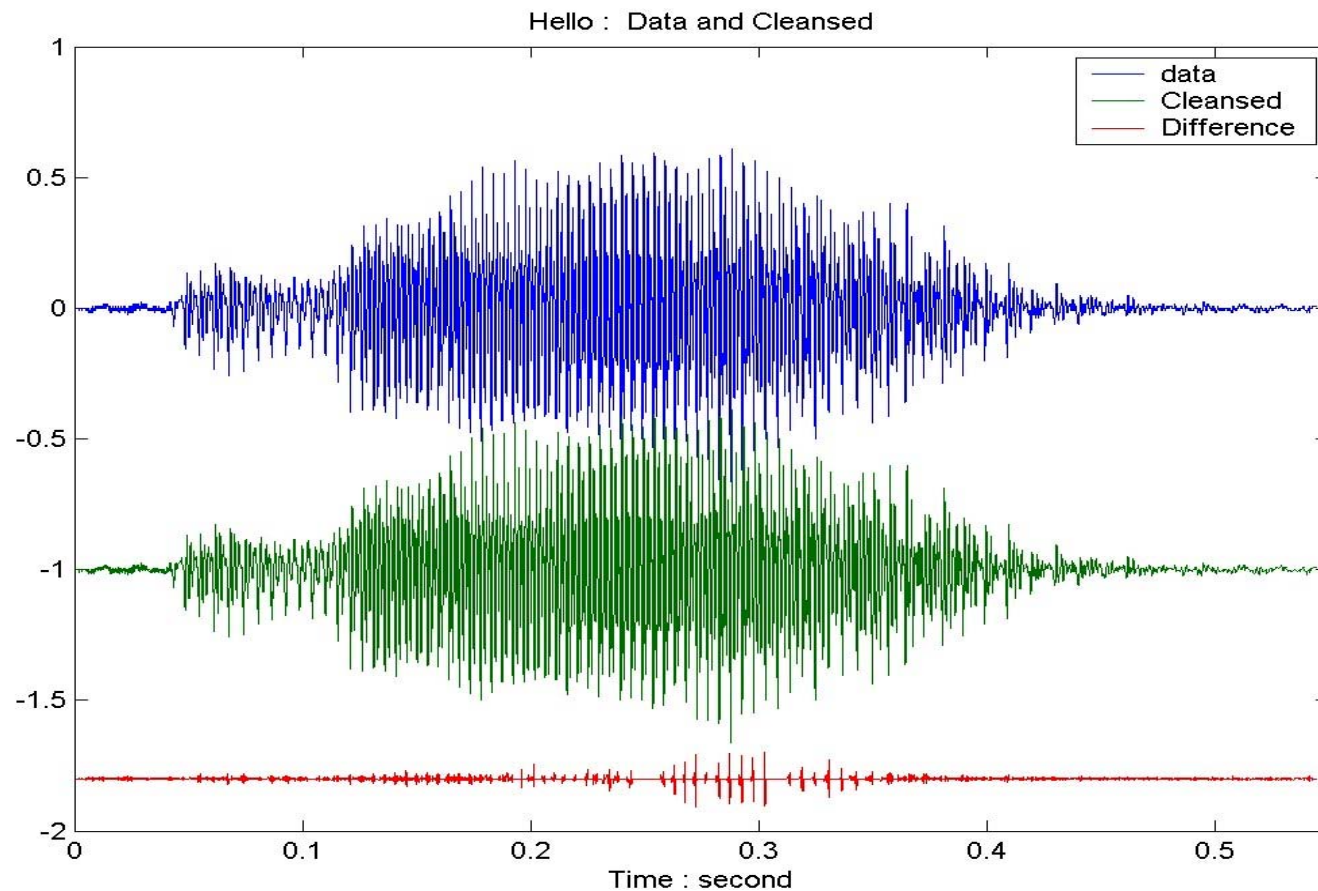


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# EMD as Filters : The Effects of Harmonics

# Speech Analysis :

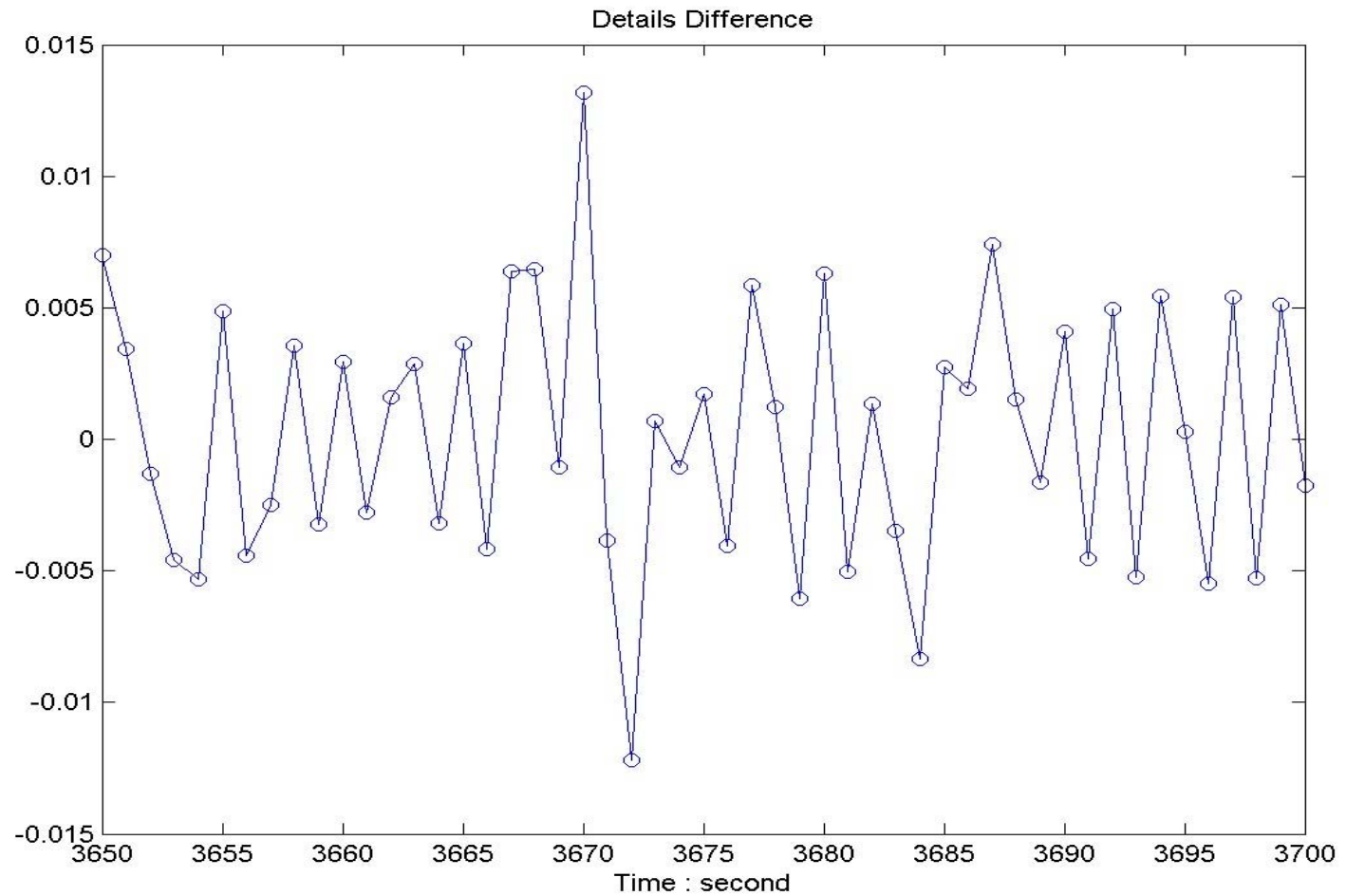
## Hello : The Effects of Harmonics and EMD filtering





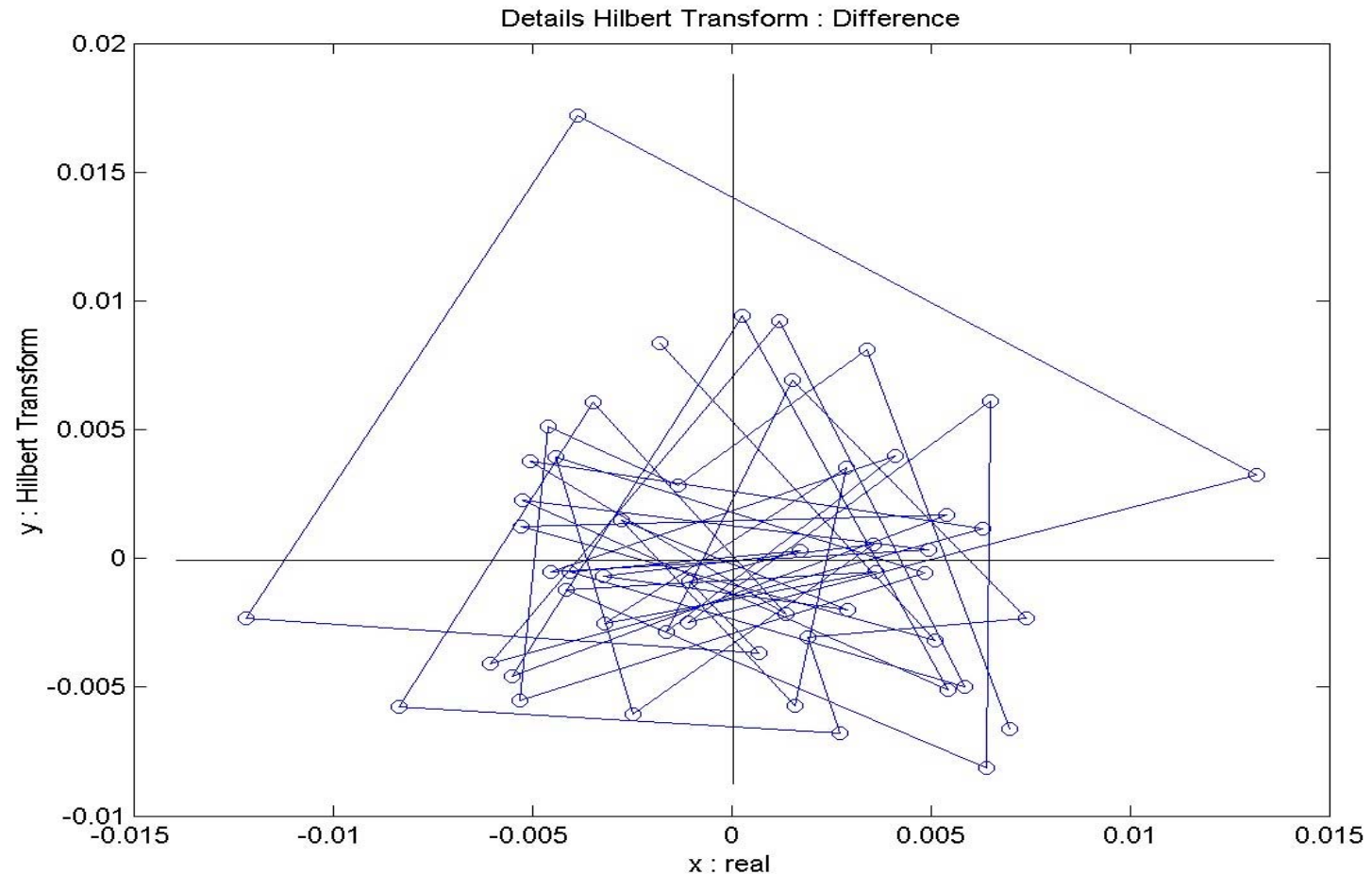
# Speech Analysis :

## Hello : Details of the Difference Data



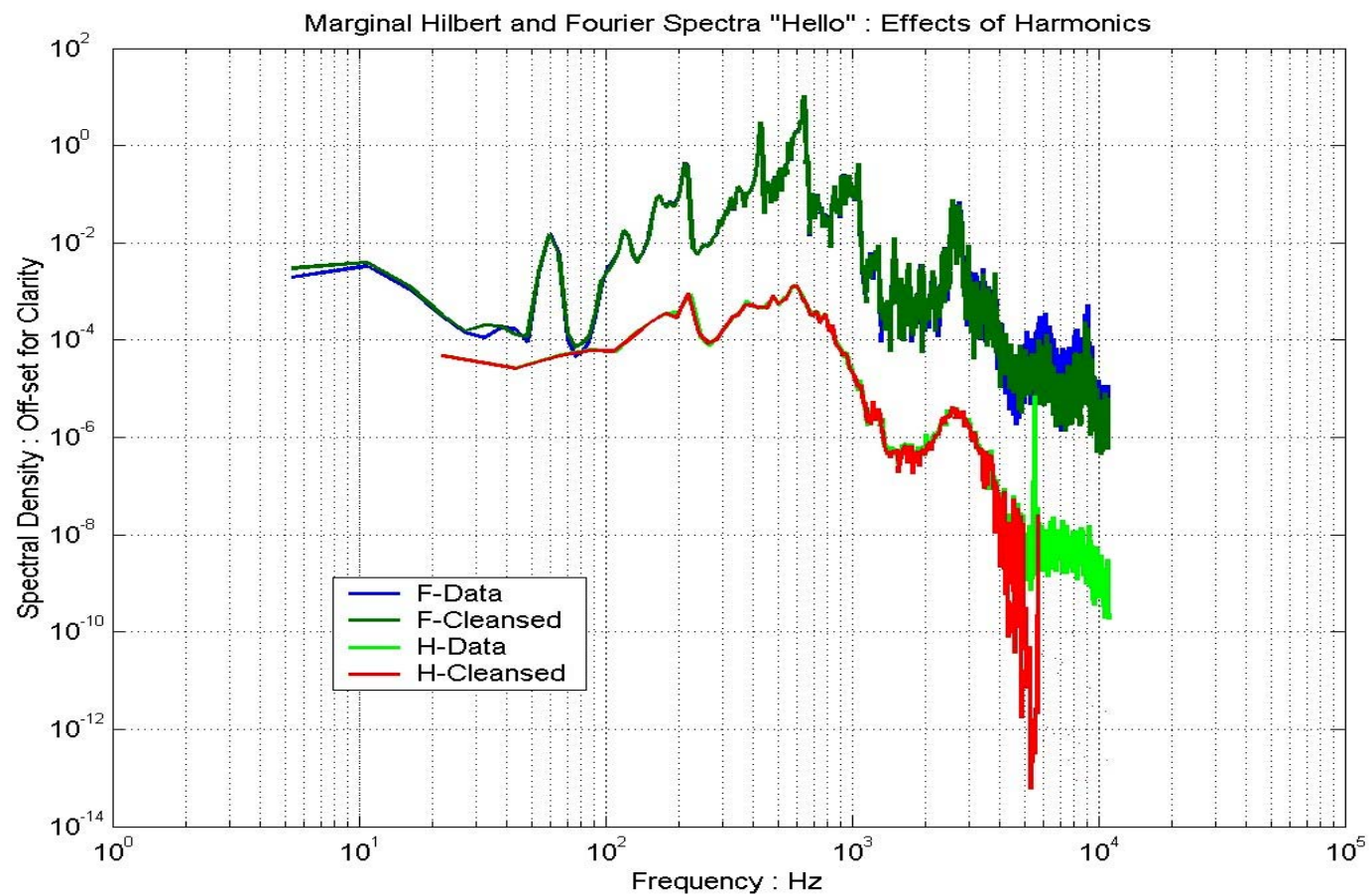
# Speech Analysis :

## Hello : The Hilbert Transform of the Difference Data



# Speech Analysis :

## Hello : The Effects of Harmonics and EMD filtering



# Summary

- **Numerous application possibilities**
- **Intellectual property protected**
- **Concepts demonstrated in many applications**
- **Licensing and partnering opportunity**
- **Enabling technology with significant commercial potential**
- **Significant benefits**
  - Precision, flexibility, accuracy, easy implementation,

# Contact Info

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- **E-mail:**  
**[evette.r.conwell@nasa.gov](mailto:evette.r.conwell@nasa.gov)**